

# Structural and electronic properties of $\text{Sb}_n\text{Al}^{(0, \pm 1)}$ ( $n = 1-10$ ) clusters using density-functional theory



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## ABSTRACT

We used the density functional theory (DFT) with the unrestricted B3LYP exchange-correlation potential and LanL2DZ basis sets to optimize the geometries of  $\text{Sb}_n\text{Al}$  and  $\text{Sb}_n\text{Al}^{\pm 1}$  ( $n = 1-10$ ) clusters. We mainly utilized Gaussian 03 W software to calculate the data. In order to find the most stable structure of each isomer, we calculated the total energy, the spin multiplicity (S), point group symmetry (PG), the electronic state (State), and the average bond lengths of Sb-Al bond and Sb-Sb bond ( $R_1$  and  $R_2$ ). Through the calculations and analysis of these data, we found the ground state structure of each group isomer. By discussing the average binding energy ( $E_b$ ), fragmentation energy ( $E_f$ ), and the second-order energy difference ( $\Delta_2E$ ), the stabilities of the  $\text{Sb}_n\text{Al}^{(0, \pm 1)}$  clusters were studied. The results of the electron transfer show that the  $\text{Sb}_4\text{Al}$  and  $\text{Sb}_8\text{Al}$  clusters are different with the other neutral clusters. In order to study the electric properties of  $\text{Sb}_n\text{Al}^{(0, \pm 1)}$  clusters, the energy gap ( $E_g$ ) between the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO), AEA, VDE, AIP, and VIP were calculated. Besides, the magnetic moment of the positive and negative clusters have the same effects when  $n = 2-9$ .

## 1. Introduction

Over that last few decades, interest in clusters arise, in part, because they constitute a new type of material that may have properties, which are distinct from those of individual atoms and molecules or bulk matters, in terms of electronic structures, geometries, magnetisms and optical properties [1–4]. Specially, there are continuous interests in metal clusters due to their great potential applications in many fields, such as catalysis, optics, and nanoelectronics [5–11]. At present, due to the special electronic structure of the p-region elements, the application of materials constructed from p-region elements become important and crosses a wide range of areas [12]. In particular, due to the especial electronic structure of the p-region element, these elements and its oxide are widely used in photolytic water [13]. Therefore, among the many clusters,  $d^{10}$  configuration clusters (Ga, Ge, In, Sb and Sn) have been studied by many scientists due to their extensive application in catalytic materials, especially in photocatalytic water.

Sb element is one of the members of  $d^{10}$  configurations, Doping and pure antimony clusters have been studied by many researchers [14–23]. For example, Polak, with his partner, had studied the affinity of some antimony clusters [20]. They found that the  $\text{Sb}_2^-$  photoelectron spectrum displayed rich vibrational and electronic structure. Hagelberg and his team had demonstrated by Hartree-Fock method that some antimony clusters had the lowest energy in what structure [22]. Zhou *et al* had studied the structural and electronic properties of  $\text{Sb}_n$  ( $n = 2-10$ ) clusters [23]. They used the density function calculation in generalized gradient

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approximation to study the structures and electronic properties of antimony clusters. And they discussed the size dependence of binding energies, the gaps between lowest-unoccupied and highest-occupied molecular orbitals, and the second-order difference of total energies.

Generally, the doping atom largely influences the electronic properties of the host clusters. For instance, when the Ti atom is doped to  $Ga_n$  clusters, the average binding energies exhibit a sequence as  $Ga_nTi^- > Ga_nTi^+ > Ga_nTi > Ga_n^{+1}$ , and the HOMO–LUMO gaps of  $Ga_nTi$  clusters are distinctly higher than those of  $Ga_n^{+1}$  clusters [24]. Obviously, the aluminum atom doping to other pure clusters have also a great impact to other pure clusters on property [25–29]. For instance, for doped zirconium clusters and pure zirconium clusters, as for the magnetism, the doping of Al atoms causes the spin-on moment of the host zirconium cluster to decrease [25]. Moreover, with respect to the detection of CO molecules at different levels with  $Zn_{12}O_{12}$  clusters and their aluminum-doped forms, replacing a Zn atom with an Al atom slightly increases its reactivity and strongly increases its sensitivity to CO molecules [28]. As a result of the difference of electronegativity, Zhao *et al* found that about 0.5 electron transfers from the 3p orbital of Al to the 6s orbital of Au atom through the study of the natural bond orbital analysis of  $Au_nAl$  clusters at their lowest-energy geometries [29].

Based on the study on hydrogen production from aluminum group cluster and water molecule, Ziebarth et al. studied [30] the interaction of Ga, In and Sn doped aluminum clusters and water molecules. They found that the speed and the amount of hydrogen production were significantly increased in the Al–Sn cluster, and they thought that the phenomenon was mainly due to the incorporation of the p-region metal with the  $d^{10}$  configuration in the aluminum cluster. The basic idea of this method that a cluster can therefore be assigned as a superatom analog of a specific group of the periodic table on the basis of the difference between its valence electron count and the number of electrons required to fill the nearest superatomic shell. One intriguing class of clusters, termed “superatomic”, has been shown to mimic the properties of elements [31]. To our knowledge, there is no theoretical study for Al-doped Sb clusters so far. In this present paper, the structural, electronic and magnetic properties are investigated within DFT framework for small  $Sb_nAl^{(0, \pm 1)}$  ( $n = 1-10$ ) clusters.

## 2. Computation details

In this article, the density functional theory (DFT) with the unrestricted B3LYP exchange-correlation potential [32,33] and LanL2DZ basis sets [34] were used to optimize the geometries of  $Sb_nAl$  ( $n = 1-10$ ) and  $Sb_nAl^{\pm 1}$  ( $n = 1-10$ ) clusters with different spin configurations. And the standard LanL2DZ basis sets provided an effective way to reduce difficulties in calculations of two-electron integrals caused by heavy TM atom were employed. In order to test the reliability of our calculations by the standard LanL2DZ basis sets, we compared our results with experimental results and other theory values for the bond length ( $R_e$ ), vibrational frequencies ( $\omega_e$ ) and ionization potentials (IPs) of the  $Sb_2$  dimer and  $Al_2$  dimer, collected in Table 1. Results were calculated for B3LYP, B3P86, B3PW91 methods and LanL2DZ, SDD basis sets, respectively. For  $Sb_2$ , the B3P86/SDD and B3PW91/SDD results for the bond length ( $R_e = 2.522 \text{ \AA}$  for B3P86/SDD,  $R_e = 2.524 \text{ \AA}$  for B3PW91/SDD) and the vibrational frequencies ( $\omega_e = 278.4 \text{ cm}^{-1}$  for

**Table 1**

The computed spin multiplicities, bond lengths ( $R_e$ ), vibrational frequencies ( $\omega_e$ ), and ionization potentials (IP) of dimers ( $Sb_2$ , and  $Al_2$ ) and available experimental and previous theoretical data.

Molecule	Method		Spin	$R_e$ (Å)	$\omega_e$ ( $\text{cm}^{-1}$ )	IP(eV)	
$Sb_2$	B3LYP	LanL2DZ	1	2.552	263.3	9.26	
		SDD	1	2.529	273.6	8.78	
	B3PW91	LanL2DZ	1	2.547	267.4	9.35	
		SDD	1	2.524	277.9	8.90	
	B3P86	LanL2DZ	1	2.545	268.0	9.89	
		SDD	1	2.522	278.4	9.43	
	Theory		1 <sup>a</sup>	2.55 <sup>b</sup>	276 <sup>b</sup>	8.78 <sup>a</sup>	
	Experiment		1 <sup>c</sup>	2.342 <sup>c</sup>	270.0 <sup>c</sup>	9.28 <sup>c</sup>	
	$Al_2$	B3LYP	LanL2DZ	3	2.855	235.1	5.87
			SDD	3	2.590	280.9	6.16
B3PW91		LanL2DZ	3	2.834	246.4	6.04	
		SDD	3	2.569	297.8	6.41	
B3P86		LanL2DZ	3	2.839	245.9	6.54	
		SDD	3	2.561	300.0	6.91	
Theory			3 <sup>i</sup>	2.7 <sup>i</sup>	241.2 <sup>i</sup>	6.12 <sup>d</sup>	
Experiment			3 <sup>k</sup>	2.7 <sup>k</sup>	284.2 <sup>k</sup>	5.98 <sup>e</sup>	

<sup>a</sup> Ref [35]

<sup>b</sup> Ref [23]

<sup>c</sup> Ref [16]

<sup>i</sup> Ref. [36]

<sup>d</sup> Ref. [37]

<sup>k</sup> Ref. [38]

<sup>e</sup> Ref. [39].

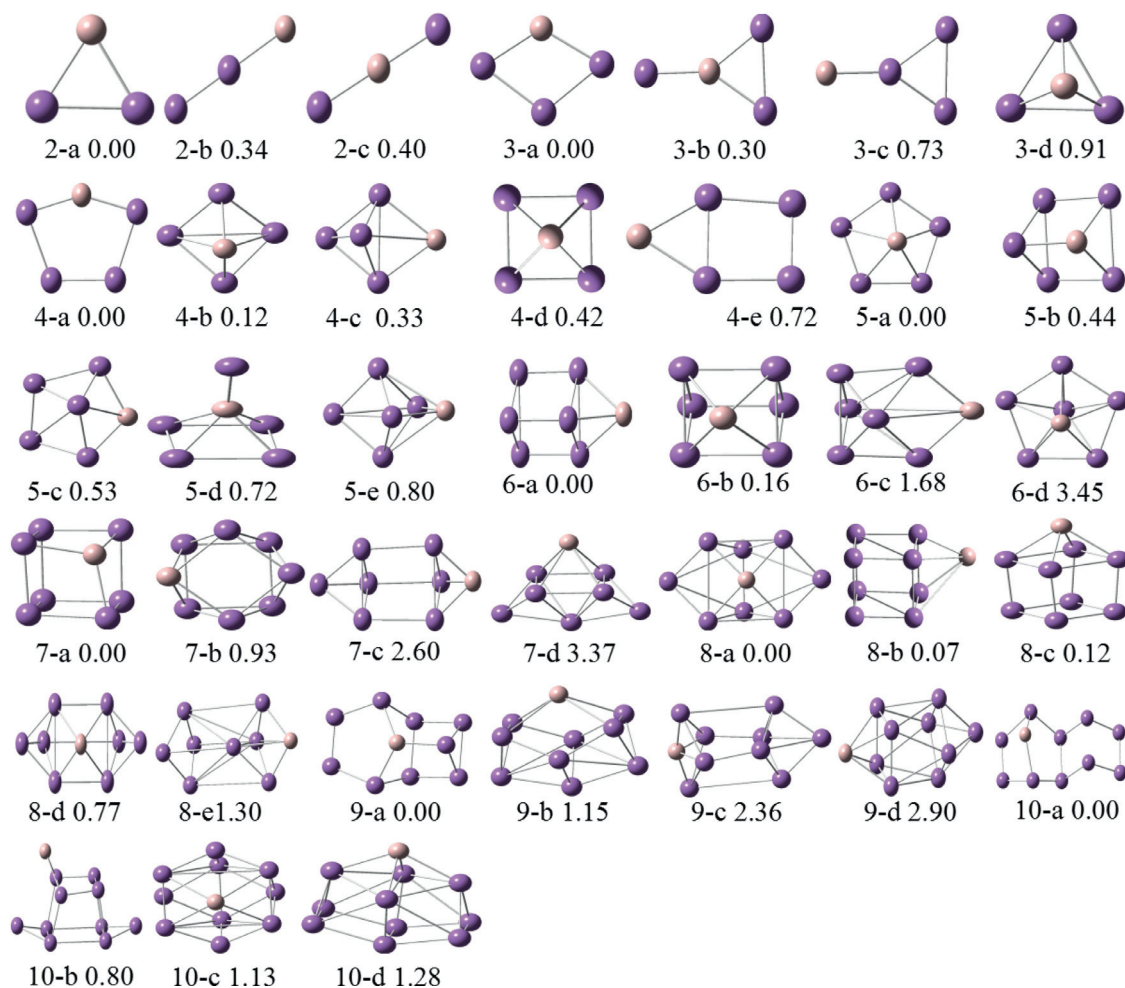


Fig. 1. The isomers structures of  $Sb_nAl$  clusters with  $n = 1-10$ .

B3P86/SDD,  $\omega_e = 277.9 \text{ cm}^{-1}$  for B3PW91/SDD) are very different from the experimental values ( $R_e = 2.342 \text{ \AA}$  [16],  $\omega_e = 270.0 \text{ cm}^{-1}$  [16]). As for  $Al_2$ , the B3P86/SDD and B3PW91/SDD results for the bond length ( $R_e = 2.561 \text{ \AA}$  for B3P86/SDD,  $R_e = 2.569 \text{ \AA}$  for B3PW91/SDD) is far from the experimental values ( $R_e = 2.7 \text{ \AA}$  [38]). From the Table 1, for  $Sb_2$ , the B3LYP/ LanL2DZ level yield  $R_e = 2.552 \text{ \AA}$ ,  $\omega_e = 263.3 \text{ cm}^{-1}$ , and IP = 9.26 eV, for  $Al_2$ , the B3LYP/ LanL2DZ level yield  $R_e = 2.855 \text{ \AA}$ ,  $\omega_e = 235.1 \text{ cm}^{-1}$ , and IP = 5.87 eV, which are more consistent with the experimental value, correspondingly. And the discussion suggests that the B3LYP/ LanL2DZ level is in excellent agreement with experimental results and other theory values.

During the process of choosing initial structures of the  $Sb_nAl$  clusters, we also considered the possible of isomeric structures. Then, based some independent configurations, we optimized several isomeric structures by placing an Al atom on each possible site of the  $Sb_n$  cluster or by adding one Sb atom to the  $Sb_{n-1}Al$  cluster as well as by substituting one Sb by Al atom form the  $Sb_{n+1}$  cluster, we obtained the lowest energy structures of  $Sb_nAl$  clusters. We also implemented configurations calculations to gain ground state structures of  $Sb_nAl^{\pm 1}$  ( $n = 1-10$ ) clusters. In order to accurately obtain the most stable geometries of  $Sb_{n-1}Al$  clusters, the possible spin multiplicities were also considered for overall isomers. For each isomer, the spin electronic configuration is considered at least from spins  $S = 1, 3, \text{ and } 5$ , when  $n$  is an odd number. And the spin electronic configuration is considered at least from spins  $S = 2, 4, \text{ and } 6$ , when  $n$  is even. All these calculations were carried out with the Gaussian 03 W package [40].

### 3. Results and discussion

#### 3.1. Structures properties

The above approaches in part two have been found to be proven powerful and identified the ground states of nanoclusters. In this section, we would research the lowest energy structures of  $Sb_nAl$  ( $n = 1-10$ ) and its low-lying isomers of  $Sb_nAl$  ( $n = 1-10$ ). And we

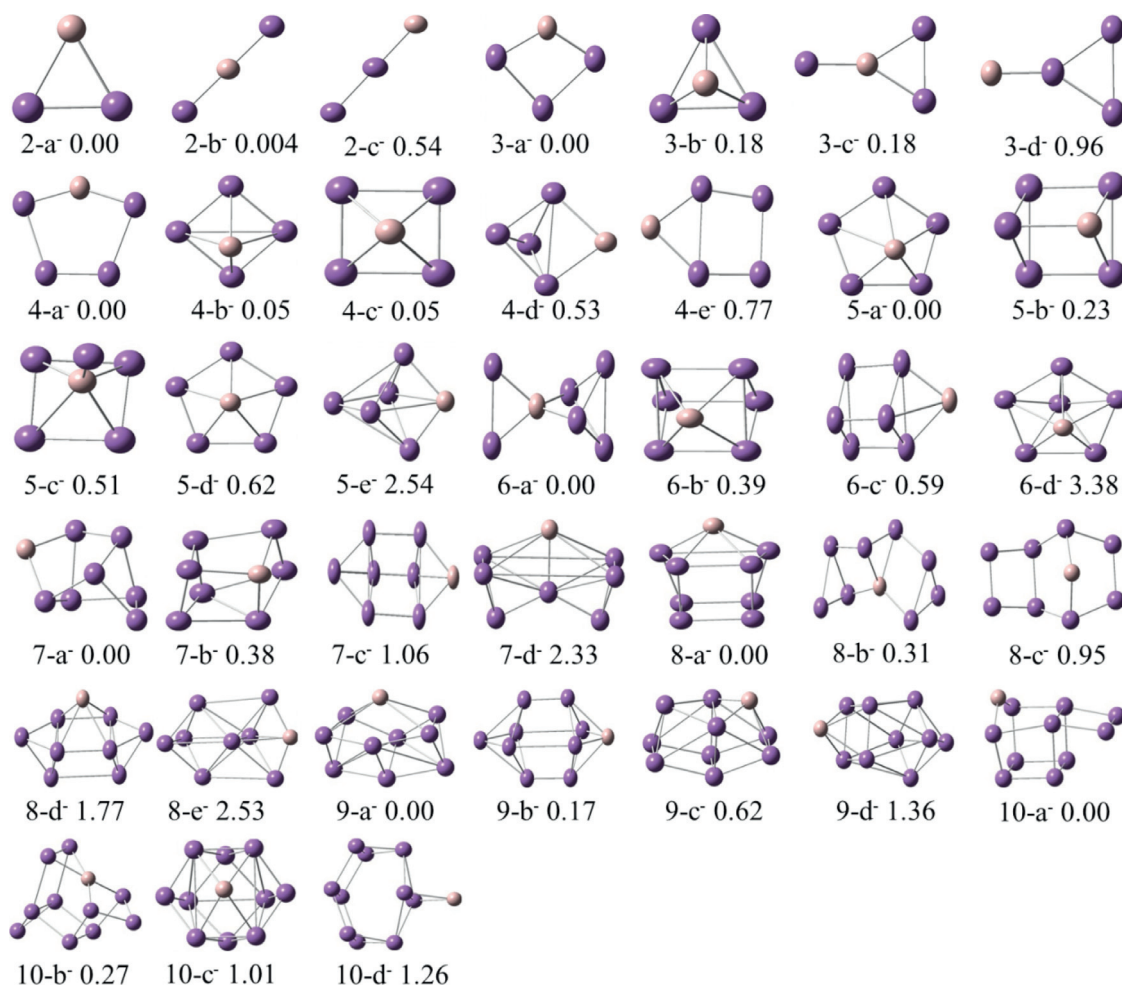


Fig. 2. The isomers structures of  $Sb_nAl^-$  clusters with  $n = 1-10$ .

used the computation scheme described in Sec. II to calculate these structures. The geometry structures of  $Sb_nAl$  ( $n = 1-10$ ) and its isomers were depicted in Fig. 1. (1) For these strings below the each model, the first one (number) represents the number of Sb atoms in the cluster, and the other ranks the isomer in the descending order of the binding energy. (2) In the picture, the atom Sb is shown as a purple sphere, and the other ball of color is Al. (3) The isomers are labeled as a, b, c, d and e in increasing order of their total energies or, equivalently, decreasing order of their relative stabilities). To compute the electron affinities of  $Sb_nAl$  ( $n = 1-10$ ) clusters, we have also investigated the anionic  $Sb_nAl^-$  clusters and cationic  $Sb_nAl^+$  up to  $n = 10$ . The lowest energy structures obtained for  $Sb_nAl^-$  and  $Sb_nAl^+$  are shown in Fig. 2 and 3, respectively. For these structures, we calculated its spin multiplicities (S), point group symmetries (PG), the average bond length of Sb-Al bond ( $R_1$ ), the average bond length Sb-Sb bond ( $R_2$ ), and the corresponding electronic state (Sta), which are listed in Table 2. We had performed an extensive search to find the minimum energy structure in the way. In the case, for each  $n$  value, we first established some higher symmetry clusters model, and then we used the software of Gaussian to optimize and calculate each model. Finally, we selected some representative and lower energy clusters (shown in the Fig. 1, Fig. 2 and Fig. 3).

### 3.1.1. $SbAl$ , $SbAl^-$ and $SbAl^+$

As for the  $SbAl^{(0, \pm 1)}$  clusters, they possess  $C_{\infty v}$  symmetry. For the  $SbAl$  dimer, the average bond length of Sb-Al ( $R_1$ ) is 2.618 Å, the bond energy is 0.68 eV. The electronic state of  $SbAl^-$  is  $^2\Sigma$ , the bond energy and the average bond length for  $SbAl^-$  are 1.34 eV and 2.496 Å, respectively. In regard to  $SbAl^+$  dimer with  $^4\Sigma$  electronic state, the 3.042 Å in average bond length and 0.33 eV in bond energy belong to them. Obviously, on the one hand, the bond energy of  $SbAl^+$  cluster is the lowest among the  $SbAl^{(0, \pm 1)}$  clusters. On the other hand, the bond length of  $SbAl^+$  is longer than the bond length of  $SbAl$  and  $SbAl^-$ . As far as the bond length and the bond energy are concerned, the Sb-Al interaction of the neutral  $SbAl$  is weaker than the Sb-Al interaction of the anionic  $SbAl^-$ .

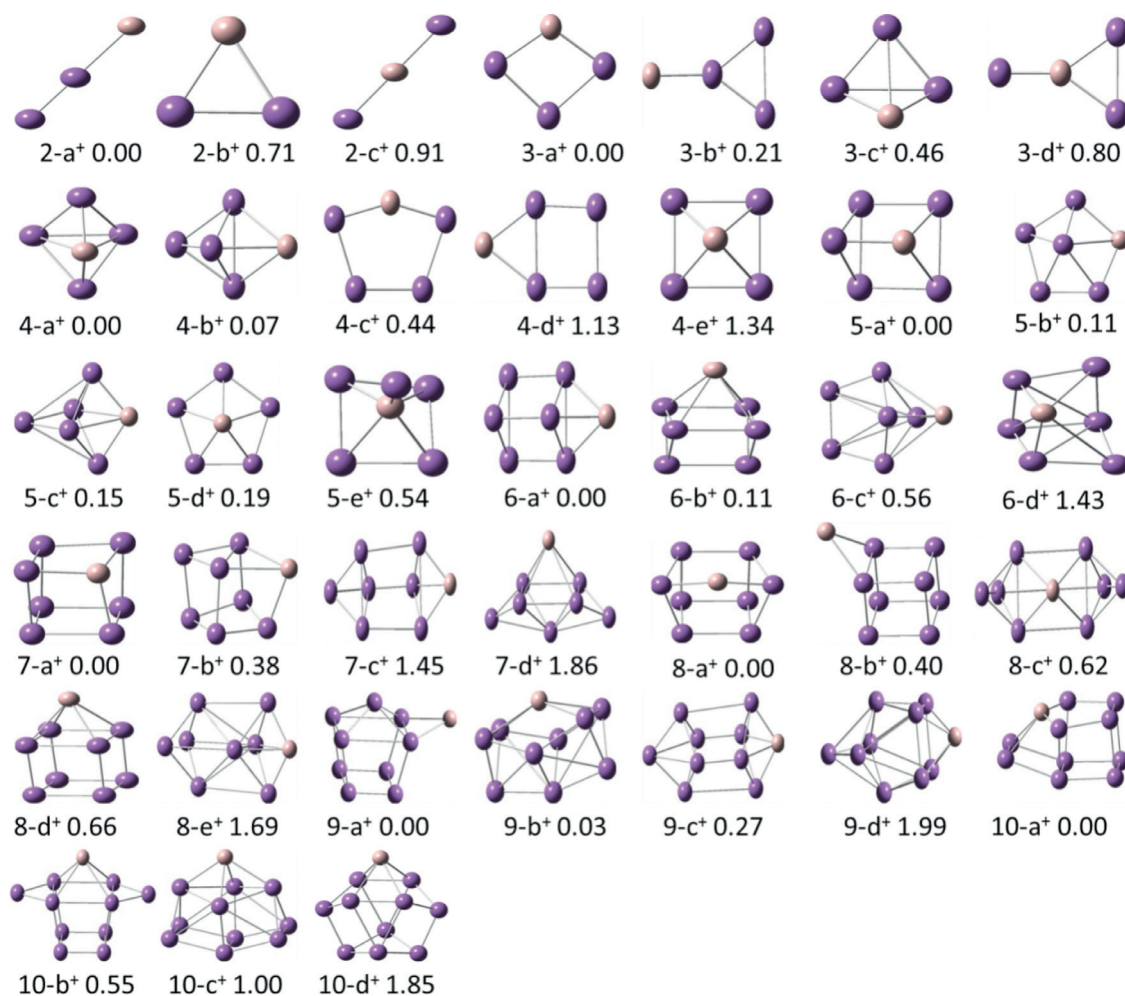


Fig. 3. The isomers structures of  $Sb_nAl^+$  clusters with  $n = 1-10$ .

### 3.1.2. $Sb_2Al$ , $Sb_2Al^-$ and $Sb_2Al^+$

With regard to  $Sb_2Al^{(0, \pm 1)}$ , that an aluminum atom interacts with two antimony atoms can form three structures including two line structures and a triangle structure. According to our calculation and optimization, the point group symmetry of the triangle structure is  $C_{2v}$ , the point group symmetries of line structures are  $D_{\infty H}$  (the Al atom between the Sb atom and the Sb atom) and  $C_{\infty v}$  (the Al atom at one end). As shown in the Fig. 1, Fig. 2 and Fig. 3, it is worth noting that the triangle structure is the lowest-energy structures for  $Sb_2Al$  cluster and  $Sb_2Al^-$  cluster. Nevertheless, the line structure of the Al atom at one end is the ground state structure for  $Sb_2Al^+$ . About triangle structure  $Sb_2Al$  cluster, the Al-Sb average bond length with 2.705 Å corresponding electronic state is  $^2A_1$ , the Sb-Sb bond length is 2.853 Å. Towards  $Sb_2Al^-$  clusters, the ground state structure with  $^1A_1$  electronic state is named 2-a<sup>-</sup> in Fig. 2, the Sb-Sb bond length and the Al-Sb average bond length of which are 2.761 Å, 2.936 Å, respectively. As the lowest-energy structure, the line structure (2-a<sup>+</sup>) of the Al atom at one end has  $^1\Sigma$  electronic state and 3.139 Å of Al-Sb bond length ( $R_1$ ) and 2.541 Å of Sb-Sb bond length ( $R_2$ ). According to the laws of physics, the reasons for that the  $R_1$  or the  $R_2$  is bigger or smaller than any other one being able to see easily in Table 2 is that the Al atom lose an electron, and the Al-Sb interaction becomes weaker and the Sb-Sb interaction becomes stronger. And the metastable structure named 2-b<sup>+</sup> in Fig. 3 owns  $^3B_2$  of electronic state, 0.71 eV of binding energy to 2-a<sup>+</sup>, 2.909 Å of Al-Sb bond length and 2.760 Å of Sb-Sb bond length.

### 3.1.3. $Sb_3Al$ , $Sb_3Al^-$ and $Sb_3Al^+$

In the case of  $Sb_3Al^{(0, \pm 1)}$ , the ground-state structures and some low-lying isomers are optimized and listed in Fig. 1, Fig. 2 and Fig. 3, and the calculation results about  $Sb_3Al^{(0, \pm 1)}$  are listed in Table 2. From literature [22], we can guess that the tetragonal structure is the most stable for  $Sb_3Al^{(0, \pm 1)}$  clusters. Through these models and calculations, we can see that the neutral, anionic and cationic are possessed with the same most stable structure that is a planar quadrilateral structure, marked as 3-a, 3-a<sup>-</sup> and 3-a<sup>+</sup>, respectively. And those stable structures have the same symmetry which are  $C_{2v}$ . The other three geometries are a three-dimensional

**Table 2**

The spin multiplicities (S), point group symmetries (PG), the group state (Sta), and the average bond lengths of Sb–Al bond and Sb–Sb bond ( $R_1$  and  $R_2$ ) are listed.

Neutral							Anionic						Cationic							
Clu.	Iso	PG	S	Sta	$R_1$	$R_2$	Clu.	Iso.	PG.	S	Sta	$R_1$	$R_2$	Clu.	Iso.	PG.	S	Sta	$R_1$	$R_2$
SbAl	1-a	$C_{\infty V}$	3	–	2.618	–	SbAl <sup>–</sup>	1-a <sup>–</sup>	$C_{\infty V}$	2	$^2\Sigma$	2.496	–	SbAl <sup>+</sup>	1-a <sup>+</sup>	$C_{\infty V}$	4	$^4\Sigma$	3.042	–
Sb <sub>2</sub> Al	2-a	$C_{2V}$	2	$^2A_1$	2.705	2.853	Sb <sub>2</sub> Al <sup>–</sup>	2-a <sup>–</sup>	$C_{2V}$	1	$^1A_1$	2.936	2.761	Sb <sub>2</sub> Al <sup>+</sup>	2-a <sup>+</sup>	$C_{\infty V}$	1	$^1\Sigma$	3.139	2.541
	2-b	$C_{\infty V}$	2	–	2.776	2.627		2-b <sup>–</sup>	$D_{\infty H}$	3	$^3\Sigma_G$	2.535	–		2-b <sup>+</sup>	$C_{2V}$	3	$^3B_2$	2.909	2.760
	2-c	$D_{\infty H}$	4	–	2.601	–		2-c <sup>–</sup>	$C_{\infty V}$	3	$^3\Sigma$	2.622	2.723		2-c <sup>+</sup>	$D_{\infty H}$	5	$^5\Sigma_G$	2.735	–
Sb <sub>3</sub> Al	3-a	$C_{2V}$	1	$^1A_1$	2.667	2.861	Sb <sub>3</sub> Al <sup>–</sup>	3-a <sup>–</sup>	$C_{2V}$	2	$^2B_1$	2.596	3.009	Sb <sub>3</sub> Al <sup>+</sup>	3-a <sup>+</sup>	$C_{2V}$	2	$^2A_2$	2.830	2.909
	3-b	$C_{2V}$	3	$^3A_2$	2.666	2.817		3-b <sup>–</sup>	$C_{3V}$	2	$^2A_1$	2.797	3.056		3-b <sup>+</sup>	$C_{2V}$	2	$^2B_1$	3.006	2.866
	3-c	$C_{2V}$	3	$^3B_2$	2.770	2.903		3-c <sup>–</sup>	$C_{2V}$	2	$^2B_2$	2.686	2.786		3-c <sup>+</sup>	$C_{3V}$	2	$^2A'$	2.740	2.871
	3-d	$C_{3V}$	1	$^1A_1$	2.664	3.194		3-d <sup>–</sup>	$C_{2V}$	2	$^2A_2$	2.643	2.927		3-d <sup>+</sup>	$C_{2V}$	2	$^2B_1$	2.690	2.734
Sb <sub>4</sub> Al	4-a	$C_S$	2	$^2A''$	2.632	2.846	Sb <sub>4</sub> Al <sup>–</sup>	4-a <sup>–</sup>	$C_S$	1	$^1A'$	2.590	2.853	Sb <sub>4</sub> Al <sup>+</sup>	4-a <sup>+</sup>	$C_{2V}$	1	$^1A_1$	2.681	3.041
	4-b	$C_{2V}$	2	$^2B_2$	2.820	3.086		4-b <sup>–</sup>	$C_{2V}$	1	$^1A_1$	–	2.887		4-b <sup>+</sup>	$C_S$	1	$^1A_1$	–	3.007
	4-c	$C_{4V}$	2	$^2A_1$	3.121	2.978		4-c <sup>–</sup>	$C_{4V}$	1	$^1A$	–	2.887		4-c <sup>+</sup>	$C_S$	1	$^1A_1$	2.707	2.871
	4-d	$C_S$	2	$^2A''$	2.955	2.939		4-d <sup>–</sup>	$C_S$	1	$^1A'$	3.036	3.008		4-d <sup>+</sup>	$C_S$	1	$^1A'$	2.991	2.935
	4-e	$C_S$	2	$^2A''$	2.844	2.918		4-e <sup>–</sup>	$C_S$	1	$^1A'$	2.790	2.917		4-e <sup>+</sup>	$C_{4V}$	1	$^1A'$	2.781	3.040
Sb <sub>5</sub> Al	5-a	$C_{5V}$	1	$^1A_1$	–	2.810	Sb <sub>5</sub> Al <sup>–</sup>	5-a <sup>–</sup>	$C_{5V}$	2	$^2A$	3.108	2.850	Sb <sub>5</sub> Al <sup>+</sup>	5-a <sup>+</sup>	$C_S$	2	$^2A''$	2.766	3.060
	5-b	$C_S$	1	$1A'$	2.720	3.067		5-b <sup>–</sup>	$C_S$	2	$^2A$	2.909	3.014		5-b <sup>+</sup>	$C_S$	2	$^2A'$	3.193	3.038
	5-c	$C_S$	1	$1A'$	2.964	3.032		5-c <sup>–</sup>	$C_1$	2	$^2A$	2.785	2.984		5-c <sup>+</sup>	$C_S$	2	$^2A'$	2.841	3.053
	5-d	$C_S$	3	$^3A$	2.787	3.005		5-d <sup>–</sup>	$C_S$	2	$^2A''$	2.956	2.971		5-d <sup>+</sup>	$C_{5V}$	2	$^2A$	3.104	2.864
	5-e	$C_1$	3	$^3A$	2.868	2.931		5-e <sup>–</sup>	$C_S$	2	$^1A'$	3.070	3.011		5-e <sup>+</sup>	$C_1$	2	$^2A$	2.922	2.966
Sb <sub>6</sub> Al	6-a	$C_1$	2	$^2A$	3.128	3.042	Sb <sub>6</sub> Al <sup>–</sup>	6-a <sup>–</sup>	$C_{2V}$	1	$^1A_1$	2.767	2.959	Sb <sub>6</sub> Al <sup>+</sup>	6-a <sup>+</sup>	$C_1$	1	$^1A$	3.074	3.052
	6-b	$C_S$	2	$^2A''$	–	3.074		6-b <sup>–</sup>	$C_S$	1	$^1A'$	–	2.961		6-b <sup>+</sup>	$C_S$	1	$^1A'$	–	3.055
	6-c	$C_{2V}$	4	$^4A_1$	3.003	2.962		6-c <sup>–</sup>	$C_1$	1	$^1A$	3.033	3.070		6-c <sup>+</sup>	$C_{2V}$	3	$^3B_1$	2.919	2.962
	6-d	$C_{5V}$	2	$^2A_1$	3.219	3.172		6-d <sup>–</sup>	$C_{5V}$	1	$^1A_1$	–	3.140		6-d <sup>+</sup>	$C_S$	5	$^1A_1$	2.850	3.025
Sb <sub>7</sub> Al	7-a	$C_S$	3	$^1A'$	3.002	3.054	Sb <sub>7</sub> Al <sup>–</sup>	7-a <sup>–</sup>	$C_{3V}$	2	$^2A_1$	2.763	3.057	Sb <sub>7</sub> Al <sup>+</sup>	7-a <sup>+</sup>	$C_1$	2	$^2A$	2.703	3.014
	7-b	$C_{3V}$	1	$^1A_1$	2.687	3.054		7-b <sup>–</sup>	$C_1$	2	$^2A$	2.803	2.989		7-b <sup>+</sup>	$C_S$	2	$^2A'$	2.752	3.052
	7-c	$C_1$	1	$^3A$	2.740	3.014		7-c <sup>–</sup>	$C_S$	2	$^2A'$	2.843	3.102		7-c <sup>+</sup>	$C_{3V}$	2	$^2A$	–	3.022
	7-d	$C_1$	1	$^1A$	2.739	3.052		7-d <sup>–</sup>	$C_1$	2	$^2A$	2.989	2.986		7-d <sup>+</sup>	$C_1$	2	$^2A$	2.758	3.047
	7-e	$C_{2V}$	1	$^1A_1$	–	3.143		7-e <sup>–</sup>	$C_{2V}$	4	$^4A_1$	2.857	2.959		7-e <sup>+</sup>	$C_{2V}$	4	$^4B_1$	–	3.043
Sb <sub>8</sub> Al	8-a	$C_2$	2	$^2B$	2.905	2.967	Sb <sub>8</sub> Al <sup>–</sup>	8-a <sup>–</sup>	$C_1$	1	$^1A$	2.778	3.019	Sb <sub>8</sub> Al <sup>+</sup>	8-a <sup>+</sup>	$C_2$	1	$^1A$	2.690	3.058
	8-b	$C_S$	2	$^2A'$	3.028	3.051		8-b <sup>–</sup>	$C_2$	3	$^3B$	2.793	2.982		8-b <sup>+</sup>	$C_S$	1	$^1A'$	3.142	3.054
	8-c	$C_1$	2	$^2A'$	–	3.028		8-c <sup>–</sup>	$C_S$	3	$^3A''$	2.777	2.914		8-c <sup>+</sup>	$C_S$	1	$^1A'$	–	2.989
	8-d	$C_S$	2	$^2A$	3.032	3.023		8-d <sup>–</sup>	$C_S$	1	$^1A'$	3.205	2.992		8-d <sup>+</sup>	$C_1$	3	$^3A$	2.813	3.019
	8-e	$C_{2V}$	4	$^4A_2$	2.835	2.948		8-e <sup>–</sup>	$C_{2V}$	1	$^1A_1$	2.609	3.119		8-e <sup>+</sup>	$C_{2V}$	3	$^3B_1$	2.660	3.023
Sb <sub>9</sub> Al	9-a	$C_S$	1	$^1A'$	2.736	2.969	Sb <sub>9</sub> Al <sup>–</sup>	9-a <sup>–</sup>	$C_S$	2	$^2A'$	3.011	3.066	Sb <sub>9</sub> Al <sup>+</sup>	9-a <sup>+</sup>	$C_S$	2	$^2A''$	–	3.038
	9-b	$C_S$	1	$^1A'$	–	3.042		9-b <sup>–</sup>	$C_2$	2	$^2A$	2.872	3.006		9-b <sup>+</sup>	$C_S$	2	$^2A'$	–	3.071
	9-c	$C_4$	3	$^3A$	2.752	2.991		9-c <sup>–</sup>	$C_S$	2	$^2A'$	2.926	3.071		9-c <sup>+</sup>	$C_2$	2	$2-B$	2.699	3.046
	9-d	$C_{4V}$	1	$^1A_1$	–	3.023		9-d <sup>–</sup>	$C_{4V}$	2	$^2B_2$	–	3.012		9-d <sup>+</sup>	$C_{4V}$	4	$^4B_1$	2.995	3.132
Sb <sub>10</sub> Al	10-a	$C_S$	2	$^2A'$	3.120	2.938	Sb <sub>10</sub> Al <sup>–</sup>	10-a <sup>–</sup>	$C_S$	3	$^3A''$	2.690	3.063	Sb <sub>10</sub> Al <sup>+</sup>	10-a <sup>+</sup>	$C_S$	1	$^1A'$	2.939	3.057
	10-b	$C_S$	4	$^4A'$	3.006	2.984		10-b <sup>–</sup>	$C_S$	3	$^3A''$	2.843	2.959		10-b <sup>+</sup>	$C_S$	3	$^3A'$	–	3.017
	10-c	$C_{2V}$	2	$^2A_1$	–	3.089		10-c <sup>–</sup>	$C_{2V}$	1	$^1A_1$	–	3.078		10-c <sup>+</sup>	$C_{2V}$	1	$^1A_1$	3.149	3.131
	10-d	$C_{2V}$	2	$^2B_1$	3.073	3.032		10-d <sup>–</sup>	$C_{2V}$	1	$^1A_1$	3.048	3.078		10-d <sup>+</sup>	$C_{2V}$	1	$^1A_1$	–	2.987

tetrahedral structure with  $C_{3V}$  symmetry, a planar Y-shaped structure with  $C_{2V}$  symmetry (An aluminum atom in the middle of the Y-shaped structure) and another planar Y-shaped structure with  $C_{2V}$  symmetry (An aluminum atom at the end of the Y-shaped structure), severally. The difference between 3-a ( $R_1 = 2.667 \text{ \AA}$ ,  $R_2 = 2.861 \text{ \AA}$ ), 3-a<sup>–</sup> ( $R_1 = 2.596 \text{ \AA}$ ,  $R_2 = 3.009 \text{ \AA}$ ) and 3-a<sup>+</sup> ( $R_1 = 2.830 \text{ \AA}$ ,  $R_2 = 2.909 \text{ \AA}$ ) are the corresponding electronic state, which are  $^1A_1$  of 3-a,  $^2B_1$  of 3-a<sup>–</sup>,  $^2A_2$  of 3-a<sup>+</sup>.

### 3.1.4. Sb<sub>4</sub>Al, Sb<sub>4</sub>Al<sup>–</sup> and Sb<sub>4</sub>Al<sup>+</sup>

In terms of Sb<sub>4</sub>Al<sup>(0, ±1)</sup> clusters, the lowest energy structure(4-a) for neutral Sb<sub>4</sub>Al clusters is similar to the minimum energy structure(4-a<sup>–</sup>) of Sb<sub>4</sub>Al<sup>–</sup> clusters, which is a plane pentagonal structure with  $C_S$  symmetry. Unlike 4-a and 4-a<sup>–</sup>, the ground-state of cationic clusters is a hexahedron with  $C_{2V}$  symmetry. From the following figure, we can clearly see that the structure of 4-b is like the structure of 4-b<sup>–</sup>, the structure of 4-d is similar to the structure of 4-c<sup>–</sup>, the relative energy between 4-a the ground-state structure for Sb<sub>4</sub>Al cluster and 4-b having a hexahedral structure is 0.12 eV, the relative energy of 4-d with quadrangular pyramid structure is 0.42 eV higher than 4-a. This shows that 4-b and 4-d are two completely different structures. But when 4-b gets an electron into 4-b<sup>–</sup>, 4-d gets an electron into 4-c<sup>–</sup>, 4-b<sup>–</sup> and 4-c<sup>–</sup> have almost the same relative energy (0.05 eV) to the ground state (4-a<sup>–</sup>). In short 4-b<sup>–</sup> and 4-c<sup>–</sup> are almost the same structure. In cationic clusters, the ground state (4-a<sup>+</sup>) is similar to 4-b, the cluster with quadrangular pyramid structure as 4-d is 4-e<sup>+</sup>, the relative energy between 4-e<sup>+</sup> and 4-a<sup>+</sup> (1.34 eV) is greater than the relative energy between 4-d and 4-b (0.3 eV).

### 3.1.5. $Sb_5Al$ , $Sb_5Al^-$ and $Sb_5Al^+$

In so far as the  $Sb_5Al^{(0, \pm 1)}$  clusters are concerned, the lowest energy structures for neutral and anionic forms are similar and have the same symmetry ( $C_{5v}$ ), but the most stable structure of cationic cluster with  $C_s$  symmetry is different with neutral and anionic forms. The pentagonal pyramid structure as the most stable structure for  $Sb_5Al$  neutral clusters has  $^1A_1$  electronic state and 2.810 Å Sb-Sb bond length. Although the minimum energy structure for  $Sb_5Al^-$  clusters is similar to  $Sb_5Al$  clusters', their bond length ( $R_1$  and  $R_2$ ) and corresponding electronic state ( $St_a$ ) aren't identical. The  $R_1$ ,  $R_2$  and  $St_a$  of  $Sb_5Al^-$  are 3.108 Å, 2.850 Å and  $^2A$ , respectively. The most favorable geometry structure for  $Sb_5Al^+$  clusters is a triangular prism structure possessed with  $R_1 = 2.766$  Å,  $R_2 = 3.060$  Å and  $^2A'$  electronic state.

### 3.1.6. $Sb_6Al$ , $Sb_6Al^-$ and $Sb_6Al^+$

In the matter of  $Sb_6Al^{(0, \pm 1)}$ , the most stable structure of  $Sb_6Al$  cluster (6-a) is formed by using one Sb atom to replace the Al atom of the structure named 5-b and then capping one Al atom on the triangular face of triangular prism structure of  $Sb_5Al$  cluster. We have also established and optimized several isomers, which are 6-b, 6-c, and 6-d. The relative energies of 6-b, 6-c and 6-d are 0.16 eV, 1.64 eV and 3.45 eV, respectively. The relative energies of 6-b $^-$ , 6-c $^-$  and 6-d $^-$  are 0.39 eV, 0.59 eV and 3.38 eV respectively higher than the ground state (6-a $^-$ ). The bond energies of 6-b $^+$ , 6-c $^+$  and 6-d $^+$  are 0.11 eV, 0.56 eV and 1.43 eV, respectively. It is obvious that the energy change range of anionic clusters and neutral clusters are larger than that of cationic clusters.

### 3.1.7. $Sb_7Al$ , $Sb_7Al^-$ and $Sb_7Al^+$

Considering the  $Sb_7Al^{(0, \pm 1)}$  clusters have eight atoms, our calculation and optimization to models confirm our guess that the cube structure is the minimum energy structure for the  $Sb_7Al^{(0, \pm 1)}$  clusters. But, the lowest energy structure for  $Sb_7Al^-$  cluster has a small change, because  $Sb_7Al^-$  has extra electronics, the interaction of aluminum atom with antimony atoms becomes more intense, and the cube structure becomes abnormal. Surely, this phenomenon is also suitable for all other anionic clusters. The most stable structure for  $Sb_7Al$  cluster is listed in Fig. 1 with  $^1A'$  electronic state and  $C_s$  symmetry. The Al-Sb and Sb-Sb average bond lengths of 7-a are 2.739 Å and 3.054 Å, respectively. In terms of the ground state structure of  $Sb_7Al^-$  clusters (7-a $^-$ ), it has  $C_{3v}$  symmetry,  $^2A_1$  electronic state, 2.763 Å in Al-Sb average bond length and 3.057 Å in Sb-Sb average bond length. Compared with 7-a and 7-a $^-$ , the ground-state structure for  $Sb_7Al^+$  clusters (7-a $^+$ ) has a lower symmetry which is  $C_1$ . Corresponding Al-Sb average bond length, Sb-Sb average bond length, and electronic state are 2.705 Å, 3.014 Å, and  $^2A$ .

### 3.1.8. $Sb_8Al$ , $Sb_8Al^-$ and $Sb_8Al^+$

As far as the  $Sb_8Al^{(0, \pm 1)}$  clusters are concerned, we obtain five isomers, in which the spin doublet state is the spin state for the  $Sb_8Al$  clusters, in addition to the fifth structure, for which the spin state is the spin quartet state. By calculations, as to  $Sb_8Al^-$  clusters, the spin triplet state is the spin state of 8-a $^-$  and 8-b $^-$ . However, when we consider 8-c $^-$ , 8-d $^-$  and 8-e $^-$ , the spin state is singlet. As shown in the Table 2,  $Sb_8Al^+$  clusters have the spin singlet state (for 8-a $^+$ , 8-b $^+$  and 8-c $^+$ ) and the spin triplet state (for 8-d $^+$  and 8-e $^+$ ). Even if they have the same spin state, but the electronic state is not the same. For example, the corresponding electronic state for 8-d $^+$  is  $^3A$ , nevertheless, 8-e $^+$  is  $^3B_1$ .

### 3.1.9. $Sb_9Al$ , $Sb_9Al^-$ and $Sb_9Al^+$

For  $Sb_9Al^{(0, \pm 1)}$  clusters, after calculating, optimizing and selecting these model several times, we finally retained four isomers and listed them in Fig. 1, Fig. 2 and Fig. 3. With the increase in the number of atoms, the interaction between each atom is also enhanced. The binding energies are 1.71 eV, 1.79 eV, 1.54 eV for 9-a, 9-a $^-$ , and 9-a $^+$ . These ground state structures of  $Sb_9Al^{(0, \pm 1)}$  clusters are different from each other. And the lowest energy structure for  $Sb_9Al$  clusters with  $C_s$  symmetry and  $^1A'$  electronic state is completely different from the minimum energy structure for  $Sb_9Al^-$  cluster with  $C_s$  symmetry and  $^2A'$  electronic state. The most stable structure for  $Sb_9Al^+$  cluster with  $C_s$  symmetry and  $^2A'$  electronic state is not the same as the former two.

### 3.1.10. $Sb_{10}Al$ , $Sb_{10}Al^-$ and $Sb_{10}Al^+$

In consideration of  $Sb_{10}Al^{(0, \pm 1)}$  clusters, the structure named 10-a in Fig. 1 is the ground-state structure of  $Sb_{10}Al$  cluster. To our surprise, there is a great difference of structures between the isomers of  $Sb_{10}Al$ ,  $Sb_{10}Al^-$  and  $Sb_{10}Al^+$ , in short, there is almost no similar structure. Our explanation is that not only the structures of clusters are charged, but also that each atom is subjected to multi-directional forces due to the larger number of atoms. In addition to the structures of this series of clusters, let us look at their characteristic parameters. The relative energy of 10-b is 0.8 eV higher than 10-a. However, the relative energy between 10-a $^-$  and 10-b $^-$  is only 0.27 eV. The ground state is marked 10-a $^-$ , which has  $C_s$  symmetry, corresponding to electronic state,  $R_1$  and  $R_2$  are  $^3A'$ , 2.690 Å, and 3.063 Å, respectively. The most stable structure of  $Sb_{10}Al^+$  cluster possesses  $C_s$  symmetry.

## 3.2. Relative stability

In order to study the stabilities of the most stable structures in each group of isomers, we calculated the averaged binding energy ( $E_b$ ), fragmentation energy ( $E_f$ ) and the second-order energy difference ( $\Delta_2E$ ) for each ground state structure. We referred to the averaged binding energies of  $Sb_n$  clusters in Document [23] so as to find the influence of Al atom doped antimony clusters. When we were doing these calculations, we did not think about entropy term, because that, in the density functional theory, the temperature is estimated at 0 k, and the entropy of the system will be zero at absolute zero, according to the third law of thermodynamics. The values of the oretical calculations of  $Sb_nAl$ ,  $Sb_nAl^-$ , and  $Sb_nAl^+$  ( $n = 1-10$ ) clusters are defined in the following formula:

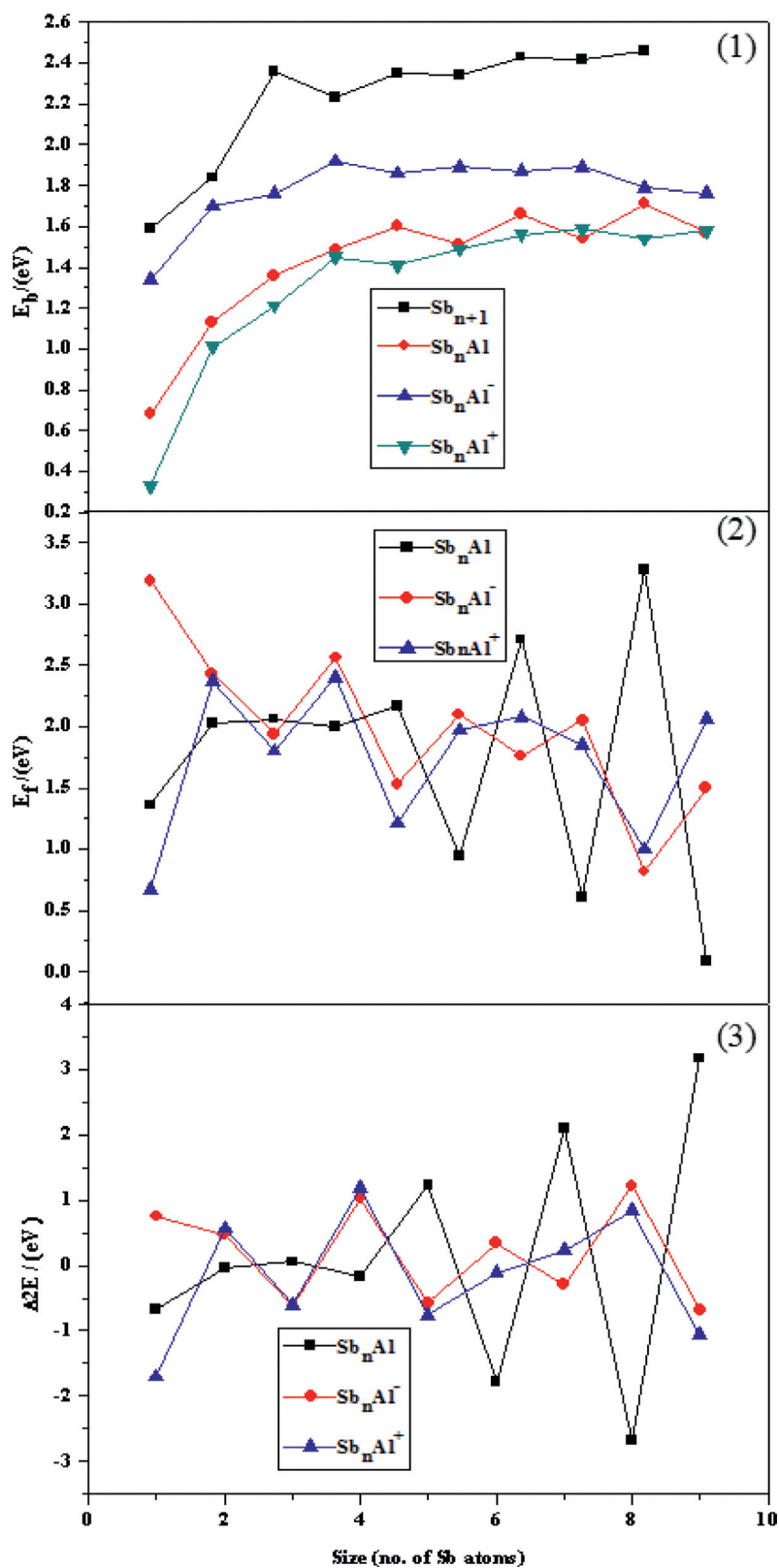


Fig. 4. Binding energies, fragmentation energies, and the second-order energy difference for the  $Sb_nAl^{(0, \pm 1)}$  ( $n = 1-10$ ) clusters versus the number of antimony atoms.

$$E_b[Sb_nAl^{(0,\pm 1)}] = (nE[Sb] + E[Al^{(0,+1)}] - E[Sb_nAl^{(0,\pm 1)}]) / (n + 1), \tag{1}$$

$$E_b[Sb_nAl^-] = ((n - 1)E[Sb] + E[Sb^-] + E[Al] - E[Sb_nAl^-]) / (n + 1), \tag{2}$$

$$E_f[Sb_nAl^{(0,\pm 1)}] = E[Sb_{n-1}Al^{(0,\pm 1)}] + E[Sb] - E[Sb_nAl^{(0,\pm 1)}], \tag{3}$$

$$\Delta_2E[Sb_nAl^{(0,\pm 1)}] = E[Sb_{n+1}Al^{(0,\pm 1)}] + E[Sb_{n-1}Al^{(0,\pm 1)}] - 2E[Sb_nAl^{(0,\pm 1)}], \tag{4}$$

here,  $E$  is the total energy of relevant system. The values of  $E_b$ ,  $E_f$  and  $\Delta_2E$  for each  $Sb_nAl$ ,  $Sb_nAl^-$ , and  $Sb_nAl^+$  clusters are shown in Figs. 4(1), 4(2) and 4(3), respectively.

First of all, we can easily see from the Fig. 4(1) that the binding energies of  $Sb_nAl^{(0, \pm 1)}$  clusters is less stable than  $Sb_{n+1}$  clusters. This phenomenon shows that the doping of Al atoms into the antimony clusters reduces the stability of the  $Sb_n$  clusters. However, the doping of Al atoms into other pure clusters does not always increase the stability of the clusters. For example, the  $Sc_n$  clusters can be more stabilized after doping Al in the host clusters in previous theoretical study [41]. Then, as seen from Fig. 4(1), as for the average binding energies of  $Sb_nAl$  clusters, when the value of  $n$  is between 4 and 10, the values of binding energy show slight oscillation. For the average binding energies of  $Sb_nAl^-$  clusters, they show an increasing trend when  $n$  is less than 4 and a decreasing trend when  $n$  is greater than 4, which means that the maximum is obtained when  $n$  is equal to 4. In general, anionic clusters have a higher averaged binding energy than neutral clusters, whose averaged binding energy is higher than those of cationic clusters.

The second, as shown in Fig. 4(2), both the charged clusters and the neutral clusters present oscillations in fragmentation energy. For neutral clusters, when  $n$  takes 3, 5 and 7, the values of fragmentation energy are at the peak of oscillation. For the  $Sb_nAl^-$  clusters, the fragmentation energies exhibit a pronounced odd-even oscillation behavior as a function of cluster size, except  $Sb_2Al^-$ . In terms of the fragmentation energies of  $Sb_nAl^+$  clusters, when  $n$  takes 4, the fragmentation energy has the maximum value that is 2.40 eV. It means that  $Sb_4Al^+$  cluster are more stable than other clusters.

The last, to further illustrate the relative stabilities of the clusters, we calculated the second-order difference energy of each ground state structure, are displayed in Fig. 4(3). When the values of  $\Delta_2E$  are positive, the dissociation of Sb atom is unfavorable process and the clusters are particularly stable. Well, in the case of  $n$  taking 3, 5, 7 and 9, the values of  $\Delta_2E$  are positive for neutral clusters. Under the situation of  $n$  taking 1, 2, 4, 6 and 8, the  $\Delta_2E$ s of anionic clusters are positive. When  $n$  is equal to 2, 4, 7 and 8, in the case of cationic clusters, the values of  $\Delta_2E$  are positive. In short, these structures are relatively stable. These cases also cater to the stability of the cluster through the binding energy.

### 3.3. Natural population analysis

We not only analyzed the structural stability in terms of energy, we also analyzed the electron transfer within each cluster. We calculated the amount of charge that each atom in the cluster by calculating the natural bond orbital (NBO) of  $Sb_{1-10}Al$  and  $Sb_{1-10}Al^{(\pm 1)}$  clusters. The total natural charges of Al atoms and the total natural charges of Sb atoms are shown in Table 3. In neutral  $Sb_nAl$  clusters, the total charge on the Al atom has a positive value (or negative value) and the total charge on the Sb atom has a negative value (or positive value), which indicates that the charge shift in the cluster. Since there is a charge transfer between the Al atom and the Sb atom, and from Table 3 we can see that the charge transfer of Sb and Al atoms are less than an electron, it indicates that the covalent bond rather than the ionic bond is formed between the Sb atom and the Al atom in the cluster.

For  $Sb_nAl^-$ , the charges on the Sb and Al atoms of  $Sb_{1-4, 8, 10}Al^-$  clusters have negative values. For  $Sb_{5-7, 9}Al^-$  clusters, the Sb atoms have negative values but Al atoms have positive values, that is to say, the electron is transferred from Al atom to Sb frames.  $Sb_nAl^+$  clusters are particularly attractive to us due to the negative charge value of Sb in  $Sb_2Al^+$  cluster. This may be caused by its special structure. From this structure, three atoms are located in the same line, and there are two Sb atoms acting on the same side of the Al atom to give the Al atom a force, however, there is no force in other directions. As a result, Sb also exhibits a negative charge, even if the entire cluster is positively charged.

**Table 3**

The total charges (Q) of Sb atoms and the charges (Q) of Al atom for the ground state structures of  $Sb_nAl^{(0, \pm 1)}$  clusters.

	Q(Sb)	Q(Al)		Q(Sb)	Q(Al)		Q(Sb)	Q(Al)
$SbAl$	-0.218	0.218	$SbAl^-$	-0.672	-0.328	$SbAl^+$	0.215	0.785
$Sb_2Al$	-0.200	0.200	$Sb_2Al^-$	-0.966	-0.034	$Sb_2Al^+$	-0.035	1.035
$Sb_3Al$	-0.094	0.094	$Sb_3Al^-$	-0.946	-0.054	$Sb_3Al^+$	0.633	0.367
$Sb_4Al$	0.032	-0.032	$Sb_4Al^-$	-0.935	-0.065	$Sb_4Al^+$	0.686	0.314
$Sb_5Al$	-0.341	0.341	$Sb_5Al^-$	-1.172	0.172	$Sb_5Al^+$	0.710	0.290
$Sb_6Al$	-0.404	0.404	$Sb_6Al^-$	-1.542	0.542	$Sb_6Al^+$	0.333	0.667
$Sb_7Al$	-0.308	0.308	$Sb_7Al^-$	-1.137	0.137	$Sb_7Al^+$	0.731	0.269
$Sb_8Al$	0.029	-0.029	$Sb_8Al^-$	-0.857	-0.143	$Sb_8Al^+$	0.714	0.286
$Sb_9Al$	-0.277	0.277	$Sb_9Al^-$	-1.066	0.066	$Sb_9Al^+$	0.255	0.745
$Sb_{10}Al$	-0.187	0.187	$Sb_{10}Al^-$	-0.860	-0.140	$Sb_{10}Al^+$	0.774	0.226

### 3.4. Electronic properties

In this section, our calculations contain the energy gap ( $E_g$ ) between the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO), the electronic properties including adiabatic electron affinity (AEA), vertical electron detachment energy (VDE), adiabatic ionization potential energy (AIP), vertical ionization potential energy (VIP). We calculated values of the AEA, VDE, AIP, and VIP using the following method.

$$AEA = E(\text{optimized neutral}) - E(\text{optimized anion}), \quad (5)$$

$$VDE = E(\text{neutral at optimized anion geometry}) - E(\text{optimized anion}), \quad (6)$$

$$AIP = E(\text{optimized cation}) - E(\text{optimized neutral}), \quad (7)$$

$$VIP = E(\text{cation at optimized neutral geometry}) - E(\text{optimized neutral}), \quad (8)$$

$$E_g = E(\text{the lowest unoccupied molecular orbital}) - E(\text{the highest occupied molecular orbital}) \quad (9)$$

here,  $E$  is the total energies of the corresponding systems. The results of our calculations about AEA, VDE, AIP, VIP, and  $E_g$  are shown in Fig. 5 (5(1), 5(2), 5(3)). First, the larger value of HOMO-LUMO energy gap is, the poorer ability of a cluster to participate in chemical reaction is. From the Fig. 5 we can also see that the stabilities of clusters with odd  $n$  are higher than the stabilities of clusters with even  $n$  in neutral clusters, except  $\text{Sb}_3\text{Al}$  cluster. In anionic clusters, it's just the opposite, the stabilities of clusters with even  $n$  are higher than the stabilities of clusters with odd  $n$ , except for  $\text{Sb}_2\text{Al}^-$  cluster. Three remarkable peaks at  $n = 1, 4,$  and  $7$  for  $\text{Sb}_n\text{Al}^+$  clusters are found, which indicate that the  $\text{SbAl}^+, \text{Sb}_4\text{Al}^+,$  and  $\text{Sb}_7\text{Al}^+$  clusters possess dramatically enhanced chemical stabilities.

From Fig. 5(2) and Fig. 5(3), Fig. 5(2) shows that the AEA and VDEs have obvious odd-even alteration as the size  $n$  increases, and the alteration behaviors are coincident from  $n = 5-10$ . This phenomenon indicates that the ionizations of the  $\text{Sb}_6\text{Al}, \text{Sb}_8\text{Al},$  and  $\text{Sb}_{10}\text{Al}$  clusters are more hard ionized than the neighbor clusters. It is seen from Fig. 5(3) that the AIPs are always larger than the VIPs. The AIPs and VIPs have obvious odd-even alteration from  $n = 4-10$ , the alteration behaviors are contrary with AEA and VDEs. We can also see that any value of AIP is greater than the value of AEA. This shows that the neutral cluster ( $\text{Sb}_n\text{Al}$ ) is more likely to get electrons into a negatively charged cluster than to lose the electron into a positively charged cluster. This phenomenon occurs not only in our calculations, but also in other articles [24,42].

### 3.5. Magnetisms

We displayed the results of the magnetic moment of ground-state clusters in Fig. 6. We can also see that the total magnetic moments of the  $\text{Sb}_n\text{Al}$  clusters show an obvious odd-even alternative behavior, when  $n$  is an odd number, the magnetic moment of the neutral cluster is zero, except for  $\text{SbAl}$  cluster. What is very interesting is that the cation clusters have the same magnetic moment as the anion clusters, when  $n$  is between 2 and 9, which also show odd-even alternative behavior, but the alternative behaviors are contrary with the neutral  $\text{Sb}_n\text{Al}$  clusters. The  $\text{SbAl}^{\pm 1}, \text{Sb}_3\text{Al}^{\pm 1}, \text{Sb}_5\text{Al}^{\pm 1}, \text{Sb}_7\text{Al}^{\pm 1},$  and  $\text{Sb}_9\text{Al}^{\pm 1}$  clusters exhibit magnetic moments, but the most stable  $\text{Sb}_2\text{Al}^{\pm 1}, \text{Sb}_4\text{Al}^{\pm 1}, \text{Sb}_6\text{Al}^{\pm 1}, \text{Sb}_8\text{Al}^{\pm 1},$  and  $\text{Sb}_{10}\text{Al}^{-1}$  clusters exhibit nonmagnetic moments, that is to say, the  $\text{SbAl}^{\pm 1}, \text{Sb}_3\text{Al}^{\pm 1}, \text{Sb}_5\text{Al}^{\pm 1}, \text{Sb}_7\text{Al}^{\pm 1}, \text{Sb}_9\text{Al}^{\pm 1},$  and  $\text{Sb}_{10}\text{Al}^{+1}$  clusters magnetic structures, the other isomers are nonmagnetic structures.

## 4. Conclusions

The geometrical and electronic properties of small Al-doped  $\text{Sb}_n$  clusters ( $n = 1-10$ ) are investigated with hybrid B3LYP functional. In this task, after our systematic study towards the  $\text{Sb}_n\text{Al}^{(0, \pm 1)}$  clusters, we obtain the following conclusion:

The geometries show that there is a certain difference between the ground state structures of  $\text{Sb}_n\text{Al}, \text{Sb}_n\text{Al}^-,$  and  $\text{Sb}_n\text{Al}^+$  clusters. When  $n$  is taken 3, the ground state of  $\text{Sb}_3\text{Al}^{(0, \pm 1)}$  clusters have the same geometry structure. When  $n$  takes other values (1, 2, 4–10), the most stable structures of  $\text{Sb}_n\text{Al}^{(0, \pm 1)}$  clusters are not the same. As the value of  $n$  increases, the bond energy roughly increases and then flattens. The fragmentation energy ( $E_f$ ) and the second-order energy difference ( $\Delta_2E$ ) show the oscillation behavior. By analyzing the relative stabilities of  $\text{Sb}_n\text{Al}^{(0, \pm 1)}$  clusters as  $n$  changes, we obtain this conclusion that the  $\text{Sb}_5\text{Al}, \text{Sb}_7\text{Al},$  and  $\text{Sb}_9\text{Al}$  clusters are relatively stable for neutral clusters,  $\text{Sb}_2\text{Al}^-, \text{Sb}_4\text{Al}^-,$  and  $\text{Sb}_7\text{Al}^-$  clusters are relatively stable for anionic clusters,  $\text{Sb}_4\text{Al}^+, \text{Sb}_6\text{Al}^+,$  and  $\text{Sb}_8\text{Al}^+$  clusters relatively stable for cationic clusters.

The natural population analysis of  $\text{Sb}_n\text{Al}$  clusters show that the charges transfer from Al atom to Sb frames, expect  $\text{Sb}_4\text{Al}$  and  $\text{Sb}_8\text{Al}$  clusters. However, the charges of  $\text{Sb}_n\text{Al}^-$  clusters on all the Sb and Al atoms have negative values, except for  $\text{Sb}_{5,7,9}\text{Al}$  clusters, and the charges of  $\text{Sb}_n\text{Al}^+$  clusters on all the Sb and Al atoms have positive values, in addition to  $\text{Sb}_2\text{Al}^+$ . After analyzing the HOMO-LUMO gaps, AEA, VDE, AIP, and VIP, the variety of HOMO-LUMO gaps both  $\text{Sb}_n\text{Al}$  and  $\text{Sb}_n\text{Al}^-$  are opposite, except for  $n = 1, 3,$  and  $10$ , the neutral  $\text{Sb}_n\text{Al}$  clusters are easier to get the electron than to lose the electron, and  $\text{Sb}_9\text{Al}$  clusters are not more easily ionized than the others. In aspect of magnetism,  $\text{Sb}_n\text{Al}^{-1}$  and  $\text{Sb}_n\text{Al}^{+1}$  clusters have the same trend of change, apart from  $\text{Sb}_{10}\text{Al}^{\pm 1}$ . Compared with  $\text{Sb}_n\text{Al}^{\pm 1}$ , the trend of change about magnetisms of  $\text{Sb}_n\text{Al}$  clusters happens to be the opposite, besides  $\text{SbAl}$ .

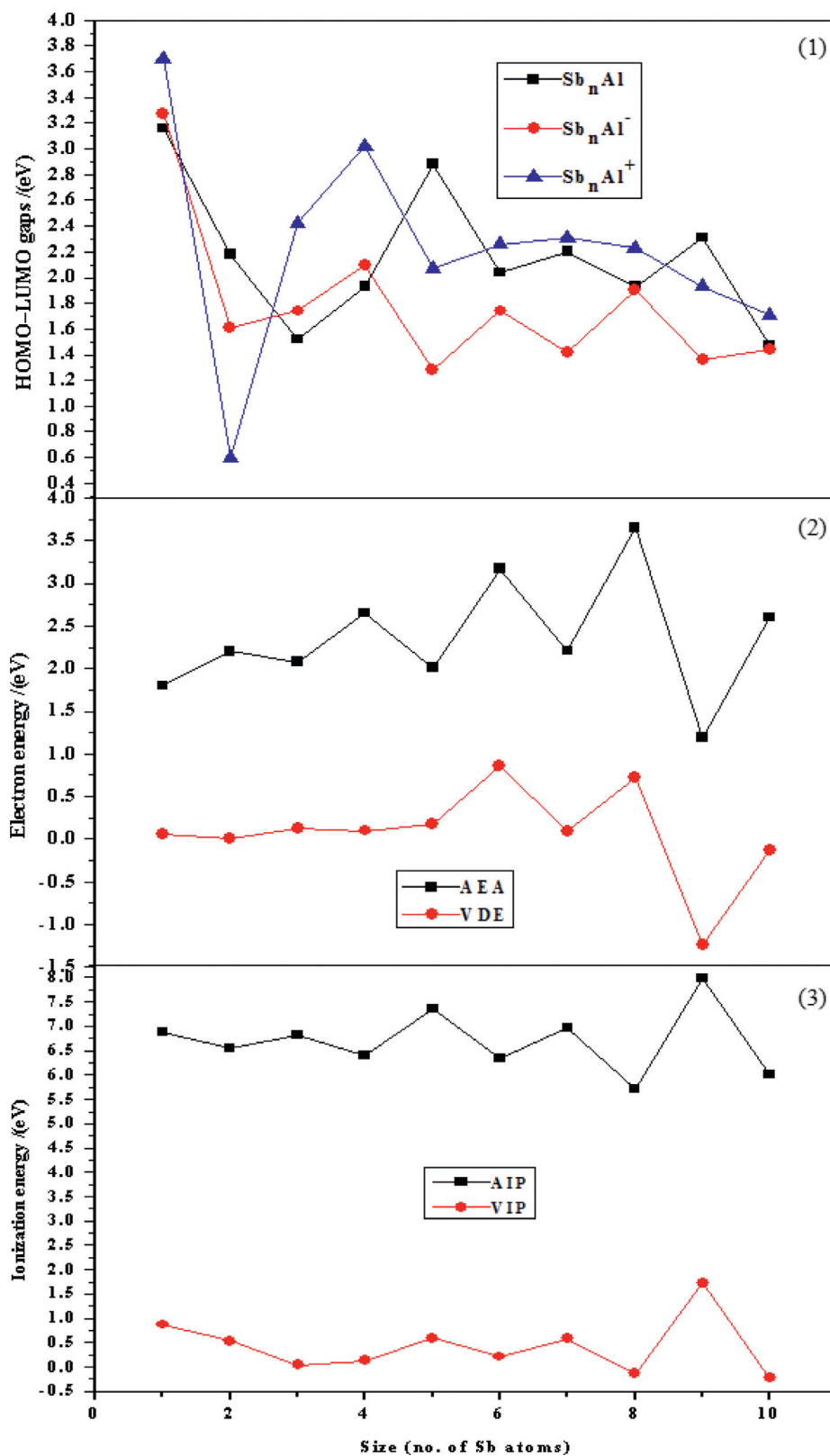


Fig. 5. HOMO-LUMO gaps, electron energies, and ionization energies for the  $Sb_nAl^{(0, \pm 1)}$  ( $n = 1-10$ ) clusters versus the number of Sb atoms.

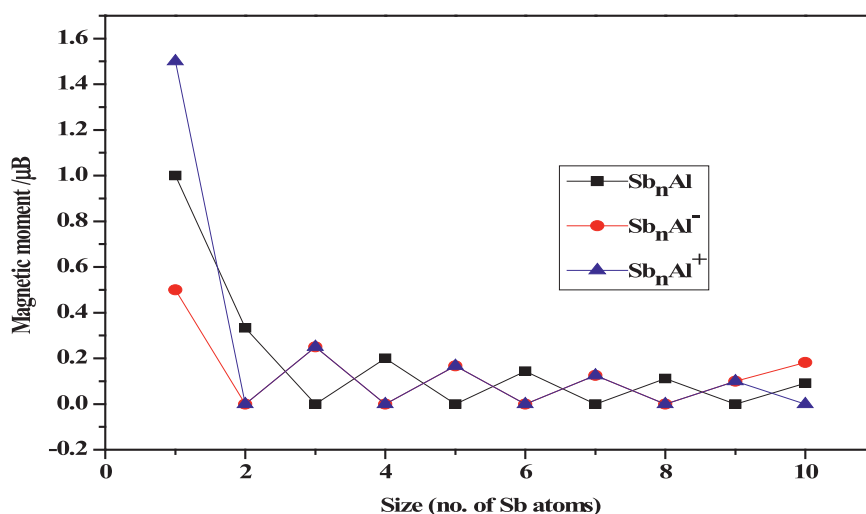


Fig. 6. Magnetic moment for the  $\text{Sb}_n\text{Al}^{(0, \pm 1)}$  ( $n = 1-10$ ) clusters versus the number of Sb atoms.

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## Supplementary materials

Supplementary material associated with this article can be found, in the online version, at [doi:10.1016/j.cjph.2018.05.003](https://doi.org/10.1016/j.cjph.2018.05.003).

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