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# Analysis of vibrational spectra of 2 and 3-methylpiperidine based on density functional theory calculations

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#### 1. Introduction

Piperidine, hexahydropyridine, is a family of heterocyclic organic compound derived from pyridine through hydrogenation. It has one nitrogen atom in the cycle. It is a clear liquid with pepper-like aroma. It boils at 106 °C, soluble in water, alcohol, and ether. The major application of piperidine is for the production of dipiperidinyl dithium tetra sulfide used as a rubber vulcanization accelerator. In pharmaceutical synthesis industry, it is used as a special solvent and a protecting group for peptide synthesis. Piperidine derivative compounds are used as intermediate to make crystal derivative of aromatic nitrogen compounds containing nuclear halogen atoms. Ring system compounds with nitrogen which have basic property play important roles as cyclic component in industrial field such as raw materials for hardener of epoxy resins, corrosion inhibitors, insecticides, accelerators for rubber, urethane catalysts, antioxidants and as a catalyst for silicone esters. They are used in manufacturing pharmaceuticals [1].

In our previous work [2], we reported the molecular structure and vibrational spectra of piperidine and 4-methylpiperidine by density functional theory calculations. In this work, we report DFT/B3LYP calculation results on 2 and 3-methylpiperidine molecules. The aim of this study is to give optimal molecular geometry, vibrational wave numbers and modes of free and deuterated species of 2 and 3 methylpiperidine and its deuterated species. The isotope effects of D atom were discussed for sensitive band to deuterated substitution.

#### ABSTRACT

The experimental and theoretical vibrational spectra of 2 and 3-methylpiperidine (abbreviated as 2-MP and 3-MP) were studied. The FT-Infrared spectra of 2-MP and 3-MP molecules were recorded in the liquid phase. The structural and spectroscopic analysis of the title molecules were made by using density functional harmonic calculations. For the title molecules, only one form was found most stable structure by using B3LYP level with the 6-311G (d,p) basis set. Selected experimental bands were assigned and characterized based on the scaled theoretical wave numbers by their total energy distribution (TED). Published by Elsevier B.V.

#### 2. Computational details

The molecular structures of 2 and 3-methylpiperidine (in vacuum) in the ground state were optimized by B3LYP with the 6-311G (d,p), 6-311++G (d,p) and cc-pVQZ basis sets. Density functional for all studies reported in this paper has the following form

$$E_{XC} = (1 - a_0)E_X^{LSDA} + a_0E_X^{HF} + a_X \Delta E_X^{B88} + a_c E_C^{LYP} + (1 - a_c)E_C^{VWN}$$

where the energy terms are the Slater exchange, the Hartree–Fock exchange, Becke's exchange functional correction, and the gradient corrected correlation functional of Lee, Yang and Parr and the local correlation functional of Vosko et al. [3]. RB3LYP with several basis sets levels of theory with the optimized geometries have been used to calculate all parameters of the title molecules.

Three sets of vibrational frequencies for these species were calculated with these methods and then scaled by corresponding scaling factors [4]. All the calculations were performed by using Gauss-view molecular visualization program and Gaussian 03 program package on the personal computer [5,6].

#### 3. Result and discussion

Piperidine has two possible chair conformations, which differ in the axial (A) or equatorial (E) position of the N–H group. Other conformations that differ from the chair (boat, envelope or twist boat) were not considered because of their high energy [7–10]. The methyl derivatives in positions  $C_2$  and  $C_3$  of the ring can have four chair conformations characterized by the relative orientations of the N–H group (A or E) and of the C–Me group (a or e) [11]. All conformations were optimized by B3LYP/6-311G (d,p) basis set. The

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		Energy (a.u.)	Energy differences (kcal/mol)	$E_{\rm HOMO}~(\rm eV)$	$E_{\rm LUMO}~(\rm eV)$	$\Delta E (\mathrm{eV})$	$\mu$ (Debye)
3MP (Chair)	Ee	-291.300655553	0.00	-6.025	1.133	7.158	1.070
	Ae	-291.299849551	0.50	-5.842	0.915	6.757	1.078
	Ea	-291.298405852	1.41	-6.021	0.970	6.991	0.915
	Aa	-291.297162924	2.19	-5.854	1.045	6.899	1.132
2MP (Chair)	Ee	-291.303288058	0.00	-6.050	1.087	7.137	0.834
	Ae	-291.302041815	0.78	-5.884	1.119	7.003	1.024
	Ea	-291.298484584	3.01	-5.912	0.919	6.831	0.815
	Aa	-291.298005869	3.31	-5.862	0.909	6.771	1.059

 $The selected \ molecular \ properties \ of \ conformation \ of \ the \ 2 \ and \ 3-methyl piperidine \ (with \ the \ B3LYP/6-311G \ (d,p)).$ 

selected molecular properties of all conformation of the 2 and 3methylpiperidine listed in Table 1. As seen in Table 1, the 2 and 3-methylpiperidine molecules show the double equatorial form as the most stable.

#### 3.1. Geometrical structures

Table 1

The optimized geometric parameters (bond lengths and bond angles) of the title molecules were given in Table 2 by using B3LYP with 6-311G (d,p), 6-311++G (d,p) and cc-pVQZ basis sets. The atomic numbering is given in Fig. 1. The molecular structures of 2 and 3-methylpiperidine have been not studied by any diffraction technique. Therefore, the molecular structure of 2 and 3-methylpiperidine were compared with those of X-ray and electron diffraction data of piperidine [10,12].

Vayner and Ball [9] give only representative bond distance, bond angles and dihedral angles, or where appropriate, ranges for the parameter type (i.e. C–H bonds). In that study the C–N–C bond angles are slightly larger than the C–C–C or N–C–C bond angles while the C–N bond distances are predicted to be slightly shorter than C–C bond distances. Our data is consistent with those observations which can be seen from Table 1.

#### 3.2. Assignment of fundamentals

The molecules of 2 and 3-methylpiperidine consist of 20 atoms, so it has 54 normal vibrational modes. The title molecules belong to  $C_1$  symmetry. The detailed vibrational assignments of fundamental modes free 2 and 3-methylpiperidine and its deuterated species along with the calculated IR intensities and normal mode description (characterized by TED) were reported in Table 3. The total energy distribution (TED) was calculated by using the Scaled Quantum Mechanic program (SQM) [13].

Chemicals were purchased from the Aldrich Chemical Company Inc., and used as received. The FT-IR spectra of the title molecules are shown in Fig. 2. The samples of 2 and 3-methylpiperidine are in liquid forms at room temperature. The FT-IR of the title molecules were recorded between 4000 cm<sup>-1</sup> and 400 cm<sup>-1</sup> region on a Mattson 1000 FT-IR spectrometer which was calibrated using polystyrene bands.

In 4000–2000 cm<sup>-1</sup> region, the vibrational spectra show characteristic bands of normal modes related to the asymmetric and symmetric stretching of the NH, CH bonds of methyl group, as well as the CH stretching modes of ring.

#### 3.2.1. NH vibration

The band recorded in the room temperature FT-IR spectrum at  $3276 \text{ cm}^{-1}$  (3MP) and  $3274 \text{ cm}^{-1}$  (2MP), are assigned to NH stretching. These bands were calculated  $3456 \text{ cm}^{-1}$ ,  $3408 \text{ cm}^{-1}$  and  $3417 \text{ cm}^{-1}$  for 3-methylpiperidine and  $3442 \text{ cm}^{-1}$ ,  $3396 \text{ cm}^{-1}$  and  $3405 \text{ cm}^{-1}$  for 2-methylpiperidine (respectively 6-311++G (d,p), 6-311G (d,p) and cc-pVQZ basis sets).

The NH stretching fundamental of piperidine was observed to the vapour band at  $3364 \text{ cm}^{-1}$  [7]. Güllüoğlu et al. [14,15] was observed to the liquid band at  $3340 \text{ cm}^{-1}$  for the NH stretching of the piperidine. The position of the methyl group in the piperidine ring influence the NH stretching wave number, which are decreased in the order 3-methylpiperidine >2-methylpiperidine in the both experimental and theoretical calculations.

The NH stretching vibration was showed shifts toward a lower wave number (~900 cm<sup>-1</sup>) in the deuterated derivative of 2 and 3-methylpiperidine. The isotopic rations ( $\upsilon_{\text{NH}}/\upsilon_{\text{ND}}$ ) were (around) 1.36 (for 2 and 3-methylpiperidine). In addition to, some vibrations ( $\upsilon_{35}$ ,  $\upsilon_{28}$ ,  $\upsilon_{21}$ ,  $\upsilon_{20}$ ,  $\upsilon_{19}$  and  $\upsilon_{10}$ , etc.) were showed a small wave number (~50 cm<sup>-1</sup>) (for 2-MP and 3-MP). These vibrations assigned at NCH bend and CN Str. Other vibrations were slightly different than its deuterated derivative. These shifts to lower values show



Fig. 1. Atomic numbering for studied molecules (in Ee conformations).

Tabl	e	2

Bond lengths and bond angles for 2 and 3-methylpiperidine (in Ee conformation).

Bond angles	2-methylp	oiperidine					3-methylp	oiperidine			
	cc-pvqz	6-311G (d,p)	6-311++G (d,p)	X-ray <sup>a</sup>	E.D. <sup>b</sup>		cc-pvqz	6-311G (d,p)	6-311++G (d,p)	X-ray <sup>a</sup>	E.D. <sup>b</sup>
$C_1 - C_2$	1.531	1.535	1.535	1.523	1.530	$C_1 - C_2$	1.531	1.535	1.535	1.523	1.530
$C_1 - H_9$	1.105	1.108	1.108	0.980	1.098	$C_1 - N_{12}$	1.460	1.463	1.464	1.464	1.461
$C_1 - N_{16}$	1.464	1.468	1.468	1.460	1.469	C1-H13	1.091	1.094	1.094	0.980	1.098
$C_1 - C_{17}$	1.522	1.526	1.526	-	-	$C_1 - H_{14}$	1.104	1.108	1.107	0.980	1.098
$C_2 - C_3$	1.531	1.535	1.535	1.523	1.530	$C_2 - C_3$	1.534	1.538	1.538	1.518	1.530
$C_2 - H_7$	1.093	1.096	1.096	0.980	1.098	$C_2 - C_{16}$	1.527	1.530	1.530	-	-
$C_2 - H_8$	1.092	1.095	1.095	0.980	1.098	$C_2 - H_{20}$	1.094	1.097	1.097	0.980	1.098
$C_3 - C_4$	1.530	1.534	1.534	1.518	1.530	$C_3 - C_4$	1.531	1.535	1.535	1.520	1.530
$C_3 - H_6$	1.091	1.094	1.094	0.980	1.098	$C_3 - H_6$	1.092	1.095	1.095	0.980	1.098
$C_3 - H_{15}$	1.094	1.097	1.097	0.980	1.098	$C_3 - H_{11}$	1.095	1.099	1.099	0.980	1.098
$C_4 - C_5$	1.526	1.530	1.530	1.520	1.530	$C_4 - C_5$	1.526	1.530	1.530	1.518	1.530
$C_4 - H_{10}$	1.092	1.095	1.095	0.980	1.098	C <sub>4</sub> –H <sub>7</sub>	1.092	1.095	1.095	0.980	1.098
C <sub>4</sub> -H <sub>11</sub>	1.091	1.094	1.094	0.980	1.098	C4-H8	1.091	1.094	1.095	0.980	1.098
C <sub>5</sub> -H <sub>12</sub>	1.090	1.093	1.093	0.980	1.098	C <sub>5</sub> -H <sub>9</sub>	1.090	1.093	1.093	0.980	1.098
C <sub>5</sub> -H <sub>13</sub>	1.103	1.107	1.106	0.980	1.098	C <sub>5</sub> -H <sub>10</sub>	1.103	1.107	1.107	0.980	1.098
C <sub>5</sub> -N <sub>16</sub>	1.460	1.464	1.464	1.461	1.469	$C_5 - N_{12}$	1.460	1.463	1.464	1.464	1.461
$H_{14} - N_{16}$	1.011	1.014	1.014	0.849	1.015	N <sub>12</sub> -H <sub>15</sub>	1.010	1.013	1.013	0.849	1.015
C <sub>17</sub> -H <sub>18</sub>	1.091	1.095	1.095	-	-	C <sub>16</sub> -H <sub>17</sub>	1.090	1.093	1.094	-	-
C <sub>17</sub> -H <sub>19</sub>	1.090	1.093	1.093	-	-	C <sub>16</sub> -H <sub>18</sub>	1.091	1.094	1.094	-	-
C <sub>17</sub> -H <sub>20</sub>	1.090	1.093	1.093	-	-	$C_{16}-H_{19}$	1.092	1.095	1.095	-	-
Bond lengths											
$C_2 - C_1 - H_9$	107.3	107.3	107.3	109.3	-	$C_2 - C_1 - N_{12}$	110.4	110.2	110.4	109.8	110.5
$C_2 - C_1 - N_{16}$	108.6	108.5	108.6	109.3	-	$C_2 - C_1 - H_{13}$	110.0	109.8	110.0	109.2	-
$H_9 - C_1 - N_{16}$	112.2	112.1	112.2	109.3	-	$C_2 - C_1 - H_{14}$	108.3	108.4	108.4	109.3	-
$C_2 - C_1 - C_{17}$	110.6	110.8	110.5	110.7	109.6	$N_{12} - C_1 - H_{13}$	108.5	108.5	108.4	109.3	-
$H_9 - C_1 - C_{17}$	108.2	108.3	108.2	-	-	$N_{12} - C_1 - H_{14}$	112.1	112.4	112.1	109.3	-
$N_{16} - C_1 - C_{17}$	109.7	109.5	109.7	-	-	$H_{13}-C_1-H_{14}$	107.1	107.2	107.2	109.4	-
$C_1 - C_2 - C_3$	111.6	111.5	111.5	110.2	109.6	$C_1 - C_2 - C_3$	109.5	109.5	109.5	110.7	109.6
$C_1 - C_2 - H_7$	108.2	108.2	108.2	109.2	-	$C_1 - C_2 - C_{16}$	111.5	111.6	111.5	-	-
$C_1 - C_2 - H_8$	109.4	109.4	109.4	109.2	-	$C_1 - C_2 - H_{20}$	106.8	100.7	100.8	109.1	-
$C_3 - C_2 - \Pi_7$	109.0	110.4	109.7	109.2	-	$C_3 - C_2 - C_{16}$	107.0	107.0	102.0	100.2	-
$C_3 - C_2 - H_8$	10.3	107.2	10.5	109.2	110.0	$C_3 - C_2 - \Pi_{20}$	107.5	107.5	108.0	109.2	-
$n_7 - c_2 - n_8$	110.0	110.0	107.5	110.2	110.0	$C_{16} - C_2 - \Pi_{20}$	108.0	100.7	100.7	110.2	- 111 1
$C_2 - C_3 - C_4$	110.3	110.3	110.3	100.3	111.1	$C_2 - C_3 - C_4$	110.0	110.0	110.0	100.5	111.1
$C_2 - C_3 - H_{17}$	10.5	109.1	109.2	109.5	_	C2-C3-H11	108.7	108.6	108.7	109.2	_
$C_2 - C_3 - H_6$	110.5	110.5	110.5	109.2	_	C <sub>2</sub> -C <sub>3</sub> -H <sub>1</sub>	110.4	110.4	110.3	109.2	_
$C_4 - C_3 - H_{17}$	109.1	109.1	109.1	109.2	_	C4-C3-H1	109.2	109.2	109.2	109.2	_
$H_{c} = C_{2} = H_{1c}$	106.5	106.5	106.5	109.2	110.0	$H_{c} = C_{2} = H_{11}$	106.4	106.4	106.4	109.2	_
	110.5	110.4	110.5	110.7	109.6		110.8	110.7	110.7	110.2	109.6
$C_3 - C_4 - H_{10}$	109.6	109.6	109.7	109.8	-	$C_3 - C_4 - H_7$	109.6	109.6	109.6	109.2	_
$C_3 - C_4 - H_{11}$	110.5	110.6	110.5	109.1	_	$C_3 - C_4 - H_8$	110.4	110.4	110.4	109.2	_
$C_5 - C_4 - H_{10}$	108.7	108.5	108.7	109.3	_	C5-C4-H7	108.6	108.5	108.7	109.3	_
$C_5 - C_4 - H_{11}$	109.8	109.9	109.7	109.3	-	$C_5 - C_4 - H_8$	109.8	109.9	109.7	109.2	_
$H_{10} - C_4 - H_{11}$	107.4	107.4	107.4	109.4	110.0	$H_7 - C_4 - H_8$	107.3	107.4	107.3	109.4	110.0
$C_4 - C_5 - H_{12}$	110.4	110.3	110.4	109.3	_	C <sub>4</sub> -C <sub>5</sub> -H <sub>9</sub>	110.4	110.3	110.4	109.2	_
$C_4 - C_5 - H_{13}$	108.7	108.8	108.8	109.3	-	$C_4 - C_5 - H_{10}$	108.8	108.8	108.8	109.2	_
$C_4 - C_5 - N_{16}$	109.8	109.6	109.8	109.8	110.5	$C_4 - C_5 - N_{12}$	109.5	109.3	109.5	109.9	110.5
$H_{12}-C_5-H_{13}$	107.1	107.2	107.2	109.4	110.0	$H_9 - C_5 - H_{10}$	107.2	107.3	107.3	109.4	110.0
$H_{12}-C_5-N_{16}$	108.4	108.4	108.4	109.3	_	$H_9 - C_5 - N_{12}$	108.6	108.5	108.5	109.3	_
$H_{13} - C_5 - N_{16}$	112.0	112.3	112.0	109.3	-	$H_{10} - C_5 - N_{12}$	112.1	112.3	112.0	109.3	-
$C_1 - N_{16} - C_5$	113.4	113.1	113.3	111.0	110.7	$C_1 - N_{12} - C_5$	112.5	112.2	112.5	111.0	110.7
$C_1 - N_{16} - H_{14}$	110.0	109.5	110.0	108.2	108.4	$C_1 - N_{12} - H_{15}$	110.4	109.9	110.4	108.2	108.4
C <sub>5</sub> -N <sub>16</sub> -H <sub>14</sub>	110.3	109.8	110.3	108.5	108.4	C5-N12-H15	110.5	110.0	110.5	108.5	108.4
C <sub>1</sub> -C <sub>17</sub> -H <sub>18</sub>	111.1	111.1	111.1	-	-	C2-C16-H17	111.0	111.0	111.0	-	-
$C_1 - C_{17} - H_{19}$	110.8	110.9	110.7	-	-	C2-C16-H18	111.4	111.4	111.4	-	-
$C_1 - C_{17} - H_{20}$	110.4	110.2	110.4	-	-	C2-C16-H19	111.1	111.2	111.2	-	-
$H_{18} - C_{17} - H_{19}$	107.6	107.6	107.6	-	-	H <sub>17</sub> -C <sub>16</sub> -H <sub>18</sub>	107.6	107.6	107.6	-	-
$H_{18} - C_{17} - H_{20}$	108.0	108.0	108.0	-	-	H <sub>17</sub> -C <sub>16</sub> -H <sub>19</sub>	107.5	107.5	107.5	-	-
$H_{19} - C_{17} - H_{20}$	108.6	108.7	108.6	-	-	H <sub>18</sub> -C <sub>16</sub> -H <sub>19</sub>	107.7	107.7	107.7	-	-

<sup>a</sup> X-ray data taken from [12].

<sup>b</sup> Electron diffraction data taken from [10].

that these NH stretching, NCH bending and NC stretching modes were sensitive to deuterated substitution.

#### 3.2.2. CH stretching vibrations

The CH stretching modes of the ring and methyl group were experimentally observed at  $2730 \text{ cm}^{-1}$ ,  $2796 \text{ cm}^{-1}$ ,  $2854 \text{ cm}^{-1}$ ,  $2919 \text{ cm}^{-1}$  and  $2933 \text{ cm}^{-1}$  for 2-methylpiperidine,  $2730 \text{ cm}^{-1}$ ,  $2800 \text{ cm}^{-1}$ ,  $2868 \text{ cm}^{-1}$  and  $2920 \text{ cm}^{-1}$  for 3-methylpiperidine.

Eleven C–H stretching modes ( $v_{42}-v_{53}$ ) were predicted in the range from 2770 cm<sup>-1</sup> to 3000 cm<sup>-1</sup> for both molecules. The C–H stretching modes of the 3-methylpiperidine were experimentally slightly larger than those of 2-methylpiperidine.

#### 3.2.3. CC-CN vibrations

The CC and CN stretching vibrations were observed at  $1317 \text{ cm}^{-1}(\text{CN Str})$ ,  $1051 \text{ cm}^{-1}(\text{CC Str})$  for piperidine [16].

#### Table 3

Comparison of the observed and calculated vibrational spectra of 2 and 3-methylpiperidine (for B3LYP calculations).

$ \begin{array}{ c  c  c  c  c  c  c  c  c  c  c  c  c $		2-Meth	ylpiperid	ine					3-Meth	ylpiperid	ine				
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		6-311+	+G (d,p)		6-311G (d,p)	cc-pVQZ	Exp. IR	TED <sup>b</sup> (%)	6-311+	+G (d,p)		6-311 G (d,p)	cc-pVQZ	Exp. IR	TED <sup>b</sup> (%)
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		NH		ND	NH	NH			NH		ND	NH	NH		
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		Freq <sup>c</sup>	IR <sup>a</sup>	Freq <sup>c</sup>	Freq <sup>d</sup>	Freq <sup>e</sup>			Freq <sup>c</sup>	IR <sup>a</sup>	Freq <sup>c</sup>	Freq <sup>d</sup>	Freq <sup>e</sup>		
bit         bit<         bit         bit<         bit< <td><math>v_1</math></td> <td>156</td> <td>0.330</td> <td>154</td> <td>153</td> <td>155</td> <td></td> <td><math>\Gamma_{\text{CNCC}}(38)</math> <math>\Gamma_{\text{CCCH}}(26)</math></td> <td>155</td> <td>0.261</td> <td>155</td> <td>152</td> <td>154</td> <td></td> <td><math>\Gamma_{\text{CCCH}}(23) \Gamma_{\text{CCCC}}(14) (\text{R-M}) \Gamma_{\text{HCCC}}(12)</math></td>	$v_1$	156	0.330	154	153	155		$\Gamma_{\text{CNCC}}(38)$ $\Gamma_{\text{CCCH}}(26)$	155	0.261	155	152	154		$\Gamma_{\text{CCCH}}(23) \Gamma_{\text{CCCC}}(14) (\text{R-M}) \Gamma_{\text{HCCC}}(12)$
$10$ $24$ $124$ $246$ $247$ $238$ $238$ $P_{exc}$ (10) $P_{excn}(10)$ $10$ $304$ $301$ $302$ $236$ $236$ $236$ $P_{exc}(10)$ $P_{excn}(12)$ $P_{exc}(10)$ $P_{excn}(12)$ $P_{exc}(10)$ $P_{excn}(12)$ $P_{exc}(10)$ $P_{excn}(12)$ $P_{exc}(10)$ $P_{excn}(12)$ $P_{exc}(10)$ $P_{exc}(10)$ $P_{excn}(12)$ $P_{exc}(10)$ <	$v_2$	218	0.270	218	216	215		$\Gamma_{\text{HCCC}}(26) \Gamma_{\text{HCCN}}(26) \Gamma_{\text{HCCH}}(11)$	208	0.081	207	206	205		$\Gamma_{\rm HCCC}$ (69) $\Gamma_{\rm HCCH}$ (19) R-M
104 $0.67$ $302$ $301$ $302$ $301$ $302$ $301$ $338$ $342$ $238$ $241$ $450$ $750$ <	$v_3$	244	1.241	239	242	241		$\Gamma_{\text{CCCH}}(15) \Gamma_{\text{CNCH}} 12 \Gamma_{\text{HCCH}}(15) (\text{R-M})$	241	0.910	237	239	238		$\Gamma_{\rm HCCC}$ (10) $\Gamma_{\rm CHCH}$ (10)
ys	$v_4$	304	0.617	302	301	302		$\delta_{\rm CCH_3}(22)\delta_{\rm NCH_3}(16)(R)\Gamma_{\rm HNCC}(12)(\rm R-M)$	299	0.140	297	296	297		$\delta_{\text{CCC}}$ (40) $\Gamma_{\text{HCCC}}$ (30) R-M
$u_{1}$ $u_{2}$ <	$v_5$	329	1.119	329	326	326		$\Gamma_{\rm CCCH}(20) \Gamma_{\rm NCCH}(12) \Gamma_{\rm NCCC}(11)$	341	1.370	331	338	338		$\Gamma_{\text{HCCC}}(18)$ $\Gamma_{\text{CHCC}}(11)$ $\Gamma_{\text{CHCH}}(13)$ $\Gamma_{\text{HCCH}}(12)$
	$v_6$	413	0.808	410	409	411		$\delta_{\rm NCC}(14) \upsilon_{\rm CC}(13)$	412	2.831	404	408	409		$δ_{\rm CCC}$ (19) $\Gamma_{\rm CCCH}$ (12) $\Gamma_{\rm CNCH}$ (10)
	$v_7$	449	2.769	432	444	446	427 vw	$\delta_{\text{CCC}}(18)$	427	2.081	425	423	423	425 vw	$\Gamma_{\rm CCCH}$ (39)
	$v_8$	474	9.206	456	470	471	458 vw	$\Gamma_{\rm HCCN}(15) \Gamma_{\rm HNCC}(13) \Gamma_{\rm CNCC}(11)$	445	4.123	439	440	442	456 vw	$\delta_{\text{CCC}}(21) \Gamma_{\text{CCCH}}(14) \Gamma_{\text{CHCH}}(11)$
	$v_9$	548	8.921	528	542	545	566 m	$\delta_{\rm NCC}(10) \Gamma_{\rm HCCC}(10)$	547	21.49	506	542	543	564 s	$\Gamma_{\text{CNCH}}(17) \delta_{\text{NCC}}(12)$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$v_{10}$	729	64.01	635	731	723	740 vs	$\upsilon_{CN}(19) \Gamma_{HNCH}(18) \Gamma_{HNCC}(16)$	735	52.42	642	738	731	747 vs	$\Gamma_{\text{HNCH}}(26) \upsilon_{\text{CC}}(22) \Gamma_{\text{HNCC}}(15) \delta_{\text{HNC}}(10)$
	$v_{11}$	773	1.050	766	766	767		$v_{\rm CC}(45) v_{\rm CN}(12)$	770	3.862	766	762	764		$v_{\rm CC}(37) + v_{\rm NC}(8)$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$v_{12}$	820	2.492	813	812	814	804 w	$\Gamma_{\rm HCCH}(13) \nu_{\rm CC}(10)$	844	3.296	819	836	837	790 vw	$v_{\rm CC}(41) + v_{\rm CN}(18)$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1/12	838	0149	825	829	831		$v_{cc}(58)$	857	5.812	850	848	850	855 s	$v_{cc}(29)$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	U14	875	0.867	858	867	868		$v_{cc}(41)\delta_{ccu}$ (15) $v_{cv}(16)$	882	1739	872	874	876	872 w	$v_{\rm NC}(24) v_{\rm CC}(13) R \delta_{\rm CCU}(16) R-M$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	14	893	5 410	882	886	887	908 m	$\Gamma_{\text{uscu}}(26) \delta_{\text{scu}}(11) \Gamma_{\text{uscu}}(10)$	894	5 481	888	887	888	912 m	$\delta_{\text{reg}}(17) \text{ R-M } \Gamma_{\text{uncu}}(12) \text{ R}$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	U <sub>15</sub>	958	1 5 8 2	932	948	950	500 m	$\mu_{\rm HCH}(20) \nu_{\rm CCH}(11) \Gamma_{\rm HNCH}(10)$	963	3 8 4 1	945	953	956	512 111	$u_{\rm loc} = (16)u_{\rm ho}(10)u_{\rm loc}(9)R-M$
$ \begin{array}{c} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 $	16	968	1.562	953	960	961		$\delta_{\text{reg}}$ (25) $u_{\text{reg}}$ (29) $u_{\text{reg}}$ (10)	969	1 915	963	959	961	960 w	$u_{eq}(24) + u_{eq}(18) + \delta_{eq}(19)R-M$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	017	006	1.302	000	086	000	092 147	$\delta_{\rm CCH_3}(25) \delta_{\rm CC}(25) \delta_{\rm CN}(10)$	086	1.515	074	076	078	078 m	$\delta_{\text{CC}}(24) + \delta_{\text{C}}(10) + \delta_{\text{CCH}}(15) \text{K}^{-10}$
$ \begin{array}{c} 19 \\ 0 & 107 \\ 0 & 107 \\ 0 & 107 \\ 0 & 107 \\ 0 & 107 \\ 0 & 107 \\ 0 & 108 \\ 0 & 117 \\ 0 & 109 \\ 0 & 107 \\ 0 & 108 \\ 0 & 108 \\ 0 & 107 \\ 0 & 108 \\ 0 & 108 \\ 0 & 107 \\ 0 & 108 \\ 0 & 108 \\ 0 & 107 \\ 0 & 108 \\ 0 & 108 \\ 0 & 107 \\ 0 & 100 \\ 0 & 107 \\ 0 & 100 \\ 0 & 107 \\ 0 & 100 \\ 0 & 107 \\ 0 & 100 \\ 0 & 107 \\ 0 & 100 \\ 0 & 107 \\ 0 & 100 \\ 0 & 107 \\ 0 & 100 \\ 0 & 107 \\ 0 & 100 \\ 0 & 107 \\ 0 & 100 \\ 0 & 107 \\ 0 & 100 \\ 0 & 107 \\ 0 & 100 \\ 0 & 107 \\ 0 & 100 \\ 0 & 107 \\ 0 & 100 \\ 0 &$	018	1040	1.740	990	1020	1021	1006 W	$O(CH_3(10) O(CH(12))$	1027	0.756	002	1027	1029	978 III 008 w	O(C(12) O(C(10)  K-W)
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	019	1040	4.114 9.45C	995 1056	1029	1051	1000 W	$U_{CC}(45)$	1057	0.750	992 1041	1027	1026	996 W	$U_{\rm CC}(55)$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$U_{20}$	1071	0.400	1050	1059	1002	1055 III	$U_{\rm CCH_3}(16) U_{\rm CN}(16) U_{\rm CC}(10)$	1000	3.190	1041	1077	1060	1055 W	$U_{\rm CCH_3}(57)U_{\rm CC}(26)$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	U <sub>21</sub>	1117	15.70	10/1	1096	1098	1085 111	$U_{CN}(22) U_{CCH_3}(15) \delta_{ring}(11)$	1111	14.67	1085	1099	1114		$U_{\rm CN}(37) U_{\rm CC}(26)$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	U <sub>22</sub>	1113	15.79	1113	1101	1102	1120 -	$U_{\rm CN}(25) U_{\rm CC}(22)$	1123	0.623	1111	1111	1114	1101 -	$\mathcal{O}_{CN}(20) \mathcal{O}_{CC}(14) \text{ K} \mathcal{O}_{HCC}(12) \text{ KIVI}$
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$v_{23}$	1144	2.231	1122	1132	1137	1120 s	$\partial_{\text{HCH}}(12)$	1146	3.118	1144	1134	1140	1121 \$	$\delta_{\rm CCH}(12)$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$v_{24}$	1153	0.786	1145	1141	1145	1157 W	$\delta_{\rm CCH}(17) \delta_{\rm NCH}(10)$	1155	7.014	1147	1142	1146	1160 s	$\delta_{\rm NCH}(19) U_{\rm NC}(14)  {\rm K}  T_{\rm CCCH}(9)  {\rm R-M}$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$v_{25}$	1218	3.129	1198	1206	1209	1224 m	$\delta_{\rm CCH}(17) U_{\rm NC}(11)$	1216	0.957	1194	1203	1206	1222 m	δ <sub>CCH</sub> (28)
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$v_{26}$	1259	2.358	1240	1246	1249		$\delta_{\rm CCH}(35) \delta_{\rm NCH}(12)  \Gamma_{\rm CCCH}(10)$	1264	0.720	1241	1249	1253		$\delta_{\rm CCH}(42) \delta_{\rm NCH}(10)$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$v_{27}$	1265	2.412	1260	1252	1255	1263 m	$\delta_{\rm CCH}(31)$	1274	3.125	1270	1261	1264	1282 m	$\delta_{\text{HCH}}(25) \delta_{\text{CCH}}(17)$
$v_{29}$ 13252.01131213111315 $\Gamma_{\rm HCCH}(4)$ $\phi_{\rm Cen}(14)$ 13101.91313011.29713011309 vw $\delta_{\rm CH}(35)$ $\Gamma_{\rm HCCH}(13)$ $v_{30}$ 13351.4221331132213281327 s $\delta_{\rm CCH}(35)$ $\Gamma_{\rm HCCH}(16)$ 13368.063131213231325 $\Gamma_{\rm HCCH}(13)$ $\delta_{\rm CCH}(10)$ $\Gamma_{\rm HCCH}(14)$ $v_{31}$ 13470.904134213341336 $\delta_{\rm CCH}(30)$ $\Gamma_{\rm HCCH}(17)$ 13440.07613441346 $\Gamma_{\rm HCCH}(20)$ $\Gamma_{\rm HCCH}(14)$ $v_{32}$ 13783.008136813631367 $\delta_{\rm CCH}(16)$ $\Gamma_{\rm HCCH}(12)$ 13570.6061347134413681376 m $\delta_{\rm HCH}(4)$ $M_{Acc}(39)$ R-M $v_{34}$ 137812.831377136713681376 s $\delta_{\rm HCH}(4)$ $M_{Acc}(3)$ R-M1382.2371366136413681376 m $\delta_{\rm HCH}(4)$ $M_{Acc}(39)$ R-M $v_{34}$ 137812.831377136713681376 s $\delta_{\rm HCH}(12)$ $M_{CCH}(11)$ M1473.987138614311437 $\Gamma_{\rm HCCH}(22)$ $\delta_{\rm HCH}(11)$ $v_{34}$ 143814431442 $M_{Acc}(14)$ $R_{Acc}(11)$ $M_{Acc}(11)$ $M_{Acc}(11)$ $M_{Acc}(11)$ $M_{Acc}(11)$ $M_{Acc}(11)$ 14551439 $\delta_{\rm HCH}(24)$ $\Gamma_{\rm HCCH}(12)$ $\delta_{\rm HCH}(12)$ $v_{34}$ 1449145114581441 $\Gamma_{\rm HCCH}(22)$ $\delta_{\rm HCH}(11)$ $M_{Acc}(12)$ $\Gamma_{\rm HCCH}(11)$ 1455146014411443 vw $\Gamma_{\rm HCCH}(22)$ $\delta_{\rm HCH}(12)$ <td< td=""><td><math>v_{28}</math></td><td>1309</td><td>9.310</td><td>1272</td><td>1295</td><td>1300</td><td>1311 vw</td><td><math>\delta_{\rm CCH}(30) I'_{\rm CNCH}(11) I'_{\rm HCCH}(10)</math></td><td>1287</td><td>8.839</td><td>1275</td><td>1272</td><td>1277</td><td></td><td><math>\delta_{\text{HCH}}(21) I'_{\text{HCCH}}(17) \delta_{\text{CCH}}(11)</math></td></td<>	$v_{28}$	1309	9.310	1272	1295	1300	1311 vw	$\delta_{\rm CCH}(30) I'_{\rm CNCH}(11) I'_{\rm HCCH}(10)$	1287	8.839	1275	1272	1277		$\delta_{\text{HCH}}(21) I'_{\text{HCCH}}(17) \delta_{\text{CCH}}(11)$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$v_{29}$	1325	22.01	1312	1311	1315		$\Gamma_{\rm HCCH}(24) \delta_{\rm CCH}(14)$	1310	1.913	1301	1297	1301	1309 vw	$\delta_{\rm CCH}(35) \Gamma_{\rm HCCH}(13)$
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$v_{30}$	1335	1.422	1331	1322	1328	1327 s	$\delta_{\rm CCH}(35) \Gamma_{\rm HCCH}(16)$	1336	8.063	1312	1323	1325		$\Gamma_{\rm HCCH}(13)  \delta_{\rm CCH}(18)  { m R}  \Gamma_{\rm HCCH}(14)  { m R-M}$
$v_{32}$ 13530.376134713391344 $\delta_{CCH}(13) \Gamma_{HCCH}(12)$ 13570.606134713441346 $\Gamma_{HCCH}(28) R-M \delta_{CCH}(21)$ $v_{33}$ 13783.008136813631367 $\delta_{CCH}(16) \Gamma \Gamma_{CNCH}(10) M$ 13783.2371366136413681376 $\delta_{HCH}(44) M \delta_{HCC}(39) R-M$ $v_{34}$ 13781.2831377136713681376 s $\delta_{HCH}(42) M \delta_{CCH}(38) R-M$ 13882.347137813761379 $\delta_{HCC}(20) \Gamma_{CNCH}(11)$ $v_{35}$ 14396.996137814241428 $\delta_{HCH}(13) R \delta_{CNH}(12) \delta_{HCH}(11) M$ 14473.987138614311437 $\Gamma_{HCCH}(22) \delta_{HNC}(20) \delta_{HCH}(11)$ $v_{35}$ 14490.680144414331437 $\delta_{HCH}(14) R \delta_{NCH}(21) \delta_{HCH}(11) R$ 14502.560144914351439 $\delta_{HCI}(23) \Gamma_{HCCH}(12) \delta_{HCH}(12)$ $v_{37}$ 14528.164145114361441 $\Gamma_{HCCH}(32) \delta_{HCI}(26)$ 14563.3791455144014441443 vw $\Gamma_{HCCH}(12) \delta_{HCI}(12) \Gamma_{HCCH}(10)$ $v_{39}$ 14662.311145014441443 sw $\Gamma_{HCCH}(23) \delta_{HCI}(26)$ 14565.1611465145014551450 $\delta_{HCI}(23) \Gamma_{HCCH}(10)$ $v_{39}$ 14601452145014551458 $\delta_{HCI}(23) \Gamma_{HCCH}(10)$ 1452145014551450 $\delta_{HCI}(23) \Gamma_{HCCH}(10)$ $v_{39}$ 14707.463146614551458<	$v_{31}$	1347	0.904	1342	1334	1336		$\delta_{\rm CCH}(30) \Gamma_{\rm HCCH}(17)$	1344	0.076	1344	1330	1335	1336 w	$\delta_{\rm CCH}(40) \Gamma_{\rm HCCH}(14)$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$v_{32}$	1353	0.376	1347	1339	1344		$\delta_{\rm CCH}(13) \Gamma_{\rm HCCH}(12)$	1357	0.606	1347	1344	1346		$\Gamma_{\rm HCCH}(28)$ R-M $\delta_{\rm CCH}(21)$
$u_{34}$ 137812.831377136713681376 s $\delta_{HCH}(42) M \delta_{CCH}(38) R-M$ 13882.347137813761379 $\delta_{HCC}(20) \Gamma_{CNCH}(11)$ $u_{35}$ 14396.996137814241428 $\delta_{HCH}(13) R \delta_{CNH}(11) M$ 14473.987138614311437 $\Gamma_{HCCH}(22) \delta_{HNC}(20) \delta_{HCH}(11)$ $u_{36}$ 14490.680144414331437 $\delta_{HCH}(14) R \delta_{HCH}(13) M \delta_{CNH}(11) R$ 14502.56014491439 $\delta_{HNC}(14) \Gamma_{HCCH}(12) \delta_{HCH}(12)$ $u_{37}$ 14528.164145114361441 $\Gamma_{HCCH}(22) \delta_{HCH}(20) \delta_{HCH}(12)$ 14503.379145514401443 vw $\Gamma_{HCCH}(23) \delta_{HCH}(12) \delta_{HCH}(12)$ $u_{38}$ 14606.3441459144414481445 s $\Gamma_{HCCH}(23) \delta_{HCH}(26)$ 14563.379145514401443 vw $\Gamma_{HCCH}(23) \delta_{HCH}(14) \Gamma_{CNCH}(10)$ $u_{38}$ 14662.211146014521454 $\delta_{CCH}(33) R-M \Gamma_{HCCC}(10) M$ 14655.16114651453 $\delta_{HCH}(43) \Gamma_{HCCC}(12) M \delta_{HCC}(12) \Gamma_{HCCH}(10)$ $u_{41}$ 14727.463146614551458 $\delta_{HCH}(21) \Gamma_{HCCH}(10) M$ 14684.304146714531455 $\delta_{HCH}(43) \Gamma_{HCCC}(12) M \delta_{HCC}(12) \Gamma_{HCC}(10)$ $u_{41}$ 14721.292147214571461 $\delta_{HCH}(21) \Gamma_{HCCH}(11) \Gamma_{CCCH}(10)$ 14755.028145714601464 $\delta_{HCH}(26) \Gamma_{HCC}(12) M \delta_{HC}(12) \Gamma_{HCC}(12) M \delta_{HC}(12) \Gamma_{HCC}(12) M \delta_$	$v_{33}$	1378	3.008	1368	1363	1367		$\delta_{\text{CCH}}(16)$ R $\Gamma_{\text{CNCH}}(14)$ $\Gamma_{\text{HCCH}}(10)$ M	1378	3.237	1366	1364	1368	1376 m	$\delta_{\text{HCH}}(44) \text{ M } \delta_{\text{HCC}}(39) \text{ R-M}$
$v_{35}$ 14396.996137814241428 $\delta_{HCH}(13) R \delta_{CNH}(12) \delta_{HCH}(11) M$ 14473.987138614311437 $\Gamma_{HCCH}(22) \delta_{HNC}(20) \delta_{HCH}(11)$ $v_{36}$ 14490.680144414331437 $\delta_{HCH}(14) R \delta_{HCH}(13) M \delta_{CNH}(11) R$ 14502.560144914351439 $\delta_{HNC}(14) \Gamma_{HCCH}(12) \delta_{HCH}(12)$ $v_{37}$ 14528.164145114361441 $\Gamma_{HCCH}(32) \delta_{HCH}(26)$ 14563.3791455144014441443 vw $\Gamma_{HCCH}(35) \delta_{HCH}(24)$ $v_{38}$ 14606.3441459144414481445 s $\Gamma_{HCCH}(28) \delta_{HCH}(19)$ 14620.038146014511458 s $\delta_{HCH}(23) \Gamma_{HACC}(10) H$ $v_{39}$ 14662.211146014521454 $\delta_{CCH}(3) R - M \Gamma_{HCCC}(10) M$ 14655.161146514551458 $\delta_{HCH}(43) \Gamma_{HCCC}(12) \Gamma_{HCC}(10)$ $v_{40}$ 14721.292147214571461 $\delta_{HCH}(28) \delta_{CHH}(16) \Gamma_{HCC}(10) M$ 14684.304146714531455 $\delta_{HCH}(43) \Gamma_{HCCC}(12) M \delta_{HCC}(12) \Gamma_{HCC}(10)$ $v_{41}$ 14721.292147214571461 $\delta_{HCH}(28) \delta_{CHH}(16) \Gamma_{HCC}(10) M$ 14684.304146714531455 $\delta_{HCH}(43) \Gamma_{HCCC}(12) M \delta_{HCC}(12) \Gamma_{HCC}(10)$ $v_{41}$ 14721.292147214571461 $\delta_{HC}(28) \Gamma_{HCC}(10) \Gamma_{HCC}(10) H$ 14755.028147514601464 $\delta_{HC}(26) \Gamma_{HCC}(12) M \delta_{HC}(12) \Gamma_{HCC}(12) $	$v_{34}$	1378	12.83	1377	1367	1368	1376 s	$\delta_{\text{HCH}}(42) \text{ M } \delta_{\text{CCH}}(38) \text{ R-M}$	1388	2.347	1378	1376	1379		$\delta_{\text{HCC}}(20) \Gamma_{\text{CNCH}}(11)$
$v_{36}$ 14490.680144414331437 $\delta_{HCH}(14) R \delta_{HCH}(13) M \delta_{CNH}(11) R$ 14502.560144914351439 $\delta_{HCC}(14) \Gamma_{HCCH}(12) \delta_{HCH}(12)$ $v_{37}$ 14528.164145114361441 $\Gamma_{HCCH}(32) \delta_{HCH}(26)$ 14563.3791455144014441443 vw $\Gamma_{HCCH}(32) \delta_{HCH}(24)$ $v_{38}$ 14606.3441459144414481445 s $\Gamma_{HCCH}(28) \delta_{HCH}(19)$ 14620.0381460144614511458 s $\delta_{HCH}(23) \Gamma_{HNCH}(14) \Gamma_{CNCH}(10)$ $v_{39}$ 14662.211146014521454 $\delta_{CCH}(33) R-M \Gamma_{HCCC}(10) M$ 14655.16114551453 $\delta_{HCH}(43) \Gamma_{HCCC}(12) \Gamma_{HCCH}(10)$ $v_{40}$ 14721.292147214571461 $\delta_{HCH}(28) \delta_{HCH}(16) \Gamma_{HCCH}(10) M$ 14684.304146714531455 $\delta_{HCH}(43) \Gamma_{HCCC}(12) M \delta_{HCC}(12) \Gamma_{HCCH}(10)$ $v_{41}$ 14721.292147214571461 $\delta_{HCH}(28) \delta_{CH}(16) \Gamma_{HCCH}(10) M$ 14684.304146714531455 $\delta_{HCH}(26) \Gamma_{HCCH}(10) M$ $v_{42}$ 281055.932810277627822730 m $v_{CH}(98)$ 282114.062821278427942730 m $v_{CH}(99)$ $v_{44}$ 293524.282935290429092854 m $v_{CH}(85)$ 292314.16292328972868 w $v_{CH}(90)$ $v_{44}$ 293524.2829362914 <td><math>v_{35}</math></td> <td>1439</td> <td>6.996</td> <td>1378</td> <td>1424</td> <td>1428</td> <td></td> <td><math>\delta_{\text{HCH}}(13) \text{ R}  \delta_{\text{CNH}}(12)  \delta_{\text{HCH}}(11)  \text{M}</math></td> <td>1447</td> <td>3.987</td> <td>1386</td> <td>1431</td> <td>1437</td> <td></td> <td><math>\Gamma_{\rm HCCH}(22)  \delta_{\rm HNC}(20)  \delta_{\rm HCH}(11)</math></td>	$v_{35}$	1439	6.996	1378	1424	1428		$\delta_{\text{HCH}}(13) \text{ R}  \delta_{\text{CNH}}(12)  \delta_{\text{HCH}}(11)  \text{M}$	1447	3.987	1386	1431	1437		$\Gamma_{\rm HCCH}(22)  \delta_{\rm HNC}(20)  \delta_{\rm HCH}(11)$
$v_{37}$ 14528.164145114361441 $\Gamma_{\text{HCCH}}(32)  \delta_{\text{HCH}}(26)$ 14563.3791455144014441443 vw $\Gamma_{\text{HCCH}}(35)  \delta_{\text{HCH}}(24)$ $v_{38}$ 14606.3441459144414481445 s $\Gamma_{\text{HCCH}}(28)  \delta_{\text{HCH}}(19)$ 14620.0381460144614511458 s $\delta_{\text{HCH}}(23)  \Gamma_{\text{HNCH}}(14)  \Gamma_{\text{CNCH}}(10)$ $v_{39}$ 14662.211146014521454 $\delta_{\text{CH}}(33)  \text{R-M}  \Gamma_{\text{HCCC}}(10)  \text{M}$ 14655.16114551453 $\delta_{\text{HCH}}(43)  \Gamma_{\text{HCCC}}(12)  \Lambda_{\text{HCCH}}(10)$ $v_{41}$ 14707.4631466145514571461 $\delta_{\text{HCH}}(28)  \delta_{\text{HCH}}(16)  \Gamma_{\text{HCCH}}(10)  \text{M}$ 14684.304146714531455 $\delta_{\text{HCH}}(43)  \Gamma_{\text{HCCC}}(12)  M_{\text{HCC}}(12)  R_{\text{HCH}}(10)$ $v_{41}$ 14721.229147214571461 $\delta_{\text{HCH}}(28)  \delta_{\text{HCH}}(10)  \Gamma_{\text{HCCH}}(10)  \text{M}$ 14684.304146714531455 $\delta_{\text{HCH}}(43)  \Gamma_{\text{HCCC}}(12)  M_{\text{HCC}}(12)  R_{\text{HCH}}(10)$ $v_{41}$ 14721.229147214571461 $\delta_{\text{HCH}}(28)  \delta_{\text{HCH}}(10)  \Gamma_{\text{HCCH}}(10)  \text{M}$ 14655.1611460145114501454 $\delta_{\text{HCH}}(43)  \Gamma_{\text{HCC}}(12)  M_{\text{HCC}}(12)  M_{\text{HCC}$	$v_{36}$	1449	0.680	1444	1433	1437		$\delta_{\text{HCH}}(14) \text{ R}  \delta_{\text{HCH}}(13) \text{ M}  \delta_{\text{CNH}}(11) \text{ R}$	1450	2.560	1449	1435	1439		$\delta_{\text{HNC}}(14) \Gamma_{\text{HCCH}}(12) \delta_{\text{HCH}}(12)$
$v_{38}$ 14606.3441459144414481445 s $\Gamma_{\rm HCCH}(28) \delta_{\rm HCH}(19)$ 14620.0381460144614511458 s $\delta_{\rm HCH}(23) \Gamma_{\rm HNCH}(14) \Gamma_{\rm CNCH}(10)$ $v_{39}$ 14662.211146014521454 $\delta_{\rm CCH}(33)  {\rm R-M}  \Gamma_{\rm HCCC}(10)  {\rm M}$ 14655.161146514501453 $\delta_{\rm HCH}(43)  \Gamma_{\rm HCCH}(12)  \Gamma_{\rm HCCH}(10)$ $v_{40}$ 14707.4631466145514551458 $\delta_{\rm HCH}(28)  \delta_{\rm HCH}(16)  \Gamma_{\rm HCCH}(10)  {\rm M}$ 14684.304146714531455 $\delta_{\rm HCH}(43)  \Gamma_{\rm HCCH}(12)  {\rm M}_{\rm HCC}(12)  {\rm R-M}$ $v_{41}$ 14721.292147214571461 $\delta_{\rm HCH}(21)  \Gamma_{\rm HCCH}(10)  {\rm M}$ 14684.304146714531455 $\delta_{\rm HCH}(43)  \Gamma_{\rm HCCH}(12)  {\rm M}_{\rm HCC}(12)  {\rm R-M}$ $v_{42}$ 2.8105.5032.8102.7762.7822.730 m $v_{\rm CH}(98)$ 2.8214.1062.8212.7842.7942.730 m $v_{\rm CH}(99)$ $v_{43}$ 2.8331002.8332.7982.8072.796 m $v_{\rm CH}(85)$ 2.8291002.8292.7932.8032.800 s $v_{\rm CH}(99)$ $v_{44}$ 2.94618.022.9462.9142.919 $v_{\rm CH}(85)$ 2.94212.262.9422.9102.914 $v_{\rm CH}(90)$ $v_{45}$ 2.9451.8.022.9462.9142.919 $v_{\rm CH}(61)v_{\rm CH}(23) {\rm M}$ 2.9482.9162.9232.920 s $v_{\rm$	$v_{37}$	1452	8.164	1451	1436	1441		$\Gamma_{\rm HCCH}(32) \delta_{\rm HCH}(26)$	1456	3.379	1455	1440	1444	1443 vw	$\Gamma_{\rm HCCH}(35) \delta_{\rm HCH}(24)$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$v_{38}$	1460	6.344	1459	1444	1448	1445 s	$\Gamma_{\rm HCCH}(28) \delta_{\rm HCH}(19)$	1462	0.038	1460	1446	1451	1458 s	$\delta_{\text{HCH}}(23) \Gamma_{\text{HNCH}}(14) \Gamma_{\text{CNCH}}(10)$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$v_{39}$	1466	2.211	1460	1452	1454		$\delta_{\rm CCH}(33)$ R-M $\Gamma_{\rm HCCC}(10)$ M	1465	5.161	1465	1450	1453		$\delta_{\text{HCH}}(43) \Gamma_{\text{HCCC}}(19) \delta_{\text{HCC}}(12) \Gamma_{\text{HCCH}}(10)$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$v_{40}$	1470	7.463	1466	1455	1458		$\delta_{\rm HCH}(28) \delta_{\rm CHH}(16) \Gamma_{\rm HCCH}(10) {\rm M}$	1468	4.304	1467	1453	1455		$\delta_{\text{HCH}}(43) \Gamma_{\text{HCCC}}(12) \text{ M} \delta_{\text{HCC}}(12) \text{ R-M}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\mathcal{U}_{41}$	1472	1.292	1472	1457	1461		$\delta_{\text{HCH}}(21) \Gamma_{\text{HCCH}}(11) \Gamma_{\text{CNCH}}(10)$	1475	5.028	1475	1460	1464		$\delta_{\text{HCH}}(26) \Gamma_{\text{HCCH}}(10)$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	U42	2810	55.93	2810	2776	2782	2730 m	$v_{\rm CH}(98)$	2821	41.06	2821	2784	2794	2730 m	$v_{\rm CH}(99)$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	U42	2833	100	2833	2798	2807	2796 m	U <sub>CH</sub> (98)	2829	100	2829	2793	2803	2800 s	U <sub>СН</sub> (99)
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1145	2935	24.28	2935	2904	2909	2854 m	$v_{\rm cu}(85)$	2923	14 16	2923	2892	2897	2868 w	$v_{cu}(90)$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1145	2946	18.02	2946	2914	2919	205 111	<i>u</i> <sub>cu</sub> (88)	2942	12.26	2942	2910	2014	2000 W	υ <sub>сп</sub> (84)
$c_{40} = 2533 + 70.05 + 2532 + 2521 + 2521 + c_{14}(01)c_{12}(25)M + 2545 + 70.05 + 2545 + 2525 + $	1140	2940	48.60	2953	2914	2913		$u_{\rm CH_2}(60)$	2942	40.09	2942	2916	2913	2920 s	$u_{\rm en}$ (90)M
	1147	2953	7084	2953	2921	2928	2919 1/147	$u_{\rm CH_3}(01) u_{\rm CH_2}(02) M$	2953	14 53	2953	2921	2926	25203	$u_{\rm en}$ (90)M

$U_{48}$	2982	52.27	2982	2950	2955		$v_{ m CH_2}(99)$	2976	46.29	2976	2944	2949		$v_{\rm CH}, (81) v_{\rm CH}(14)$
$U_{49}$	2988	34.40	2988	2954	2960		$v_{\rm CH_{2}}(97)$	2984	24.22	2984	2948	2954		$v_{cH}(91)$
$v_{50}$	2989	31.92	2989	2956	2960		$v_{ m CH}(98)$	2990	37.11	2990	2955	2961		$v_{\rm CH}(98)$
$v_{51}$	2996	56.82	2996	2964	2968	2933 vs	$v_{ m CH_2}(99)$	2994	31.30	2994	2962	2966		$v_{\mathrm{CH}}(84)$
$v_{52}$	3011	30.75	3011	2978	2983		$v_{\rm CH_3}(100){\rm M}$	3006	49.19	3006	2974	2979		$v_{\rm CH_3}(94){\rm M}$
$v_{53}$	3028	28.99	3028	2996	2999		$v_{\text{CH}}$ (66)M	3012	29.09	3012	2980	2985		$v_{\text{CH}_3}(99)$ M
$v_{54}$	3442	0.086	2518	3396	3405	3274	$v_{\rm NH}$ 100	3456	0.068	2528	3408	3417	3276 w, br	$v_{\rm NH}(100)$
R: The ri	ng of piperidin	e, M: Methyl g	roup, <i>v</i> : Stretc	thing, <i>δ</i> : Bendi	ng, <i>I</i> : Torsio	n, vw: Very weal	c, w: Weak, m: Medi	um, s: Strong,	vs: Very strong					
<sup>a</sup> Relat	ive absorption	intensities no	malized with	highest peak	absorption ec	jual to 100.								

These vibrations were observed  $1045 \text{ cm}^{-1}$  (Ring Str) for 4-methylpiperidine [2]. As seen in Table 3, seven peaks were observed in the  $740-1085 \text{ cm}^{-1}$  range, which were at  $740 \text{ cm}^{-1}$ ,  $804 \text{ cm}^{-1}$ ,  $908 \text{ cm}^{-1}$ ,  $982 \text{ cm}^{-1}$ ,  $1006 \text{ cm}^{-1}$ ,  $1055 \text{ cm}^{-1}$ and 1085 cm<sup>-1</sup> for 2-methylpiperidine. The six peaks were observed in the 747-1055 cm<sup>-1</sup> range, which were at 747 cm<sup>-1</sup>,  $790 \text{ cm}^{-1}$ ,  $912 \text{ cm}^{-1}$ ,  $978 \text{ cm}^{-1}$ ,  $998 \text{ cm}^{-1}$  and  $1055 \text{ cm}^{-1}$  for 3-methylpiperidine. These vibrations revealed to be mixed with C-C, C-N stretching and some bending vibrations. The position of the methyl group in the piperidine ring influence the CC and CN stretching wave number, which are decreased in the order 2-methylpiperidine > 3-methylpiperidine in the both experimental and theoretical calculations.

#### 3.2.4. Methylene group vibrations

For the assignments of CH<sub>2</sub> group frequencies, basically six fundamentals can be associated to each CH<sub>2</sub> group namely; CH<sub>2</sub> sy-symmetric stretch; CH<sub>2</sub> asy-asymmetric stretch; CH<sub>2</sub> sciss-scissoring; CH<sub>2</sub> rock-rocking, CH<sub>2</sub> wag-wagging and CH<sub>2</sub> twist-twisting modes of CH<sub>2</sub> group would be expected. The fundamental CH<sub>2</sub> vibrations are able to scissoring, wagging, twisting and rocking appear in the expected frequency regions  $1500-800 \text{ cm}^{-1}$ . We determined the scissoring vibrations of the CH<sub>2</sub> ( $v_{41}$ - $v_{35}$ ), the wagging vibrations of the CH<sub>2</sub> ( $v_{34}$ - $v_{29}$ ), the twisting vibrations of the CH<sub>2</sub> ( $v_{28}$ - $v_{23}$ ) and the rocking vibrations of the CH<sub>2</sub> ( $v_{18}$ - $v_{13}$ ) every one molecules.

#### 3.2.5. Methyl group vibrations

Vibrations of the methyl group in the 2 and 3-MP should be described by 12 normal modes. The CH<sub>3</sub> fundamental modes are



Fig. 2. (a) The infrared spectra of 2 and 3-methylpiperidine for under 1600 cm<sup>-1</sup> wave numbers and (b) The infrared spectra of 2 and 3-methylpiperidine for over 2600 cm<sup>-1</sup> wave numbers.

Total energy distribution calculated B3LYP/6-311++G (d,p)

Scaling factor: 0.978. Scaling factor: 0.967.

Scaling factor: 0.969

two asymmetric  $CH_3$  stretching, one symmetric  $CH_3$  stretching, two asymmetric  $CH_3$  bending, one symmetric  $CH_3$  bending, two  $CH_3$ rocking and one  $CH_3$  torsional vibrations. The C– $CH_3$  fundamental modes are one C– $CH_3$  stretch and two C– $CH_3$  bending vibrations.

For the CH<sub>3</sub> stretching vibrations, we expect to observe three bands at about 3020–2920 cm<sup>-1</sup> region. Three CH<sub>3</sub> stretching modes ( $\nu_{53}$ ,  $\nu_{52}$ ,  $\nu_{47}$ ) were predicted in this region. The Symmetric CH<sub>3</sub> stretching vibrations were observed at 2919 cm<sup>-1</sup> (2-MP) and 2920 cm<sup>-1</sup> (3-MP) in the FT-IR spectrum for free 2-MP and 3-MP molecules.

The asymmetric CH<sub>3</sub> bending bands usually occur between at 1430 cm<sup>-1</sup> and 1470 cm<sup>-1</sup> region. The asymmetric CH<sub>3</sub> bending modes ( $\nu_{40}$ ,  $\nu_{39}$ ) were predicted in the region. The asymmetric CH<sub>3</sub> bending vibrations ( $\nu_{35}$ ) were observed at 1445 cm<sup>-1</sup> (for 2MP) and 1433 cm<sup>-1</sup> (for 3MP) in the FT-IR spectra. On the other hand, the symmetric CH<sub>3</sub> bending vibration appears in the 1360–1400 cm<sup>-1</sup> region. The symmetric CH<sub>3</sub> bending vibrations ( $\nu_{34}$ ) were observed 1376 cm<sup>-1</sup> for title molecules in the FT-IR spectra [17].

The C–CH<sub>3</sub> stretching vibration was observed at 1055 cm<sup>-1</sup> for both molecules in the FT-IR spectra. This peak ( $\nu_{20}$ ) were predicted at 1071 cm<sup>-1</sup> (6-311++G (d,p)), 1059 cm<sup>-1</sup> (6-311G (d,p)) and 1062 cm<sup>-1</sup> (cc-PVQZ) for 2-methylpiperidine. In-plane C–CH<sub>3</sub> bending vibration were predicted ( $\nu_4$ ) at 304 cm<sup>-1</sup> (6-311++G (d,p)), 302 cm<sup>-1</sup> (6-311G (d,p)) and 302 cm<sup>-1</sup> (cc-PVQZ) for 2-MP. This peak were theoretical predicted at 299 cm<sup>-1</sup> (6-311++G (d,p)), 296 cm<sup>-1</sup> (6-311G (d,p)) and 297 cm<sup>-1</sup> (cc-PVQZ) for 3-MP. In-plane and out-of-plane vibrations of C–CH<sub>3</sub> were not observed in the FT-infrared spectra.

#### 4. Conclusion

The IR spectra of the title molecules were computed by the B3LYP methods in conjunction with the 6-311++G (d,p), 6-311G (d,p) and cc-pVQZ basis sets. Results were in good agreement with its observed FT-IR spectrum. The vibrational spectra provided by B3LYP functional with 6-311G (d,p) and cc-pVQZ basis sets were the closest to the experimental values. The RMS values were about  $31.62 \text{ cm}^{-1}$  for the first basis set and  $34.10 \text{ cm}^{-1}$  for the second one. The scale factors were used in order to compare how the calculated wave numbers are consistent with those of the experimental ones. By taking into account small variations of the scaling factors for the derivatives of the title molecules, for future IR spectral predictions for unknown molecules of this class, one can recommend same scaling factors for the methods mentioned above.

The isotope effects of D atom were discussed for sensitive band to deuterated substitution. The NH, CN stretching and NCH bending modes were showed shifts toward a lower wave number in the deuterated derivative of selected molecules. This means that NH, CN stretching and NCH bending modes were sensitive to deuterated coordination.

The experimental geometric parameters were in better agreement with the optimized geometric parameters. Optimized bond lengths of studied molecules were found to have a good correlation for cc-pVQZ basis set than 6-311G (d,p) and 6-311G++ (d,p) basis sets. The RMS values were 0.095 A (for cc-pVQZ basis set), 0.097 (for 6-311G (d,p) and 6-311G++ (d,p) basis sets). However, the results showed that experimental and theoretical bond angles were in good agreement for B3LYP/6-311G (d,p) level of theory.

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